Introduction	Introduction	Introduction
Hennessy-Miner Logic Correspondence between HM Logic and Strong Bisimilarity	Hennessy-Miner Logic Correspondence between HM Logic and Strong Bisimilarity	Hennessy-Minter Logic Correspondence between HM Logic and Strong Bisimilarity Kodal and Temporal Properties
	Verifying Correctness of Reactive Systems	Model Checking of Reactive Systems
Semantics and Verification 2005	Let <i>Impl</i> be an implementation of a system (e.g. in CCS syntax). Equivalence Checking Approach	
Lecture 5	<ul> <li>Impl ≡ Spec</li> <li>■ is an abstract equivalence, e.g. ~ or ≈</li> <li>Spec is often expressed in the same language as Impl</li> <li>Spec provides the full specification of the intended behaviour</li> </ul>	Our Aim Develop a logic in which we can express interesting properties of reactive systems.
<ul> <li>Hennessy-Milner logic</li> <li>syntax and semantics</li> <li>correspondence with strong bisimilarity</li> <li>examples in CWB</li> </ul>	Model Checking Approach         Impl ⊨ Property         • ⊨ is the satisfaction relation         • Property is a particular feature, often expressed via a logic         • Property is a partial specification of the intended behaviour	
Lecture 5 Semantics and Verification 2005 Introduction Hennessy-Milner Logic Correspondence between HM Logic and Strong Bisimilarity	Lecture 5 Semantics and Verification 2005 Introduction Syntax Hennessy-Miner Logic Correspondence between HM Logic and Strong Bisimilarity Denotational Semantics	Lecture 5 Semantics and Verification 2005 Introduction Syntax Hennessy-Miner Logic Correspondence between HM Logic and Strong Bisimilarity Correspondence between HM Logic and Strong Bisimilarity
Logical Properties of Reactive Systems	Hennessy-Milner Logic – Syntax	Hennessy-Milner Logic – Semantics
Modal Properties – what can happen now (possibility, necessity) <ul> <li>drink a coffee (can drink a coffee now)</li> <li>does not drink tea</li> <li>drinks both tea and coffee</li> <li>drinks both tea and coffee</li> </ul>	Syntax of the Formulae $(a \in Act)$ $F, G ::= tt   ff   F \land G   F \lor G   \langle a \rangle F   [a]F$ Intuition: $tt$ all processes satisfy this property	Let $(Proc, Act, \{ \xrightarrow{a}   a \in Act \})$ be an LTS. Validity of the logical triple $p \models F$ $(p \in Proc, F \text{ a HM formula})$ $p \models tt$ for each $p \in Proc$
<ul> <li>drinks tea after coffee</li> <li>Temporal Properties – behaviour in time</li> <li>never drinks any alcohol (safety property: nothing bad can happen)</li> </ul>	ff no process satisfies this property $\land$ , $\lor$ usual logical AND and OR $\langle a \rangle F$ there is at least one <i>a</i> -successor that satisfies F [a]F all <i>a</i> -successors have to satisfy F	$p \models \text{ff for no } p \text{ (we also write } p \not\models \text{ff)}$ $p \models F \land G \text{ iff } p \models F \text{ and } p \models G$ $p \models F \lor G \text{ iff } p \models F \text{ or } p \models G$ $p \models \langle a \rangle F \text{ iff } p \stackrel{a}{\longrightarrow} p' \text{ for some } p' \in Proc \text{ such that } p' \models F$
<ul> <li>eventually will have a glass of wine (liveness property: something good will happen)</li> <li>Can these properties be expressed using equivalence checking?</li> </ul>	Remark Temporal properties like <i>always/never in the future</i> or <i>eventually</i> are not included.	$p \models [a]F$ iff $p' \models F$ , for all $p' \in Proc$ such that $p \xrightarrow{a} p'$ We write $p \not\models F$ whenever $p$ does not satisfy $F$ .

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Introduction Hennessy-Milner Logic Correspondence between HM Logic and Strong Blaimiliarity What about Negation?	Introduction Hennessy-Milner Logic Correspondence between HM Logic and Strong Bisimilarity Hennessy-Milner Logic — Denotational Semantics	Introduction Hennessy-Milner Logic         Syntax Semantics Semantics Denotational Semantics           Correspondence between HM Logic and Strong Bisimilarity         Semantics Denotational Semantics           The Correspondence Theorem
For every formula $F$ we define the formula $F^c$ as follows: • $tt^c = ft$ • $ft^c = tt$ • $(F \land G)^c = F^c \lor G^c$ • $(F \lor G)^c = F^c \land G^c$ • $(\langle a \rangle F)^c = [a]F^c$ • $([a]F)^c = \langle a \rangle F^c$ Theorem ( $F^c$ is equivalent to the negation of $F$ ) For any $p \in Proc$ and any HM formula $F$ • $p \models F \implies p \nvDash F^c$ • $p \nvDash F \implies p \models F^c$	For a formula $F$ let $\llbracket F \rrbracket \subseteq Proc$ contain all states that satisfy $F$ . Denotational Semantics: $\llbracket . \rrbracket : Formulae \to 2^{Proc}$ • $\llbracket t \rrbracket = Proc$ • $\llbracket t \rrbracket = Proc$ • $\llbracket f \rrbracket = \emptyset$ • $\llbracket F \lor G \rrbracket = \llbracket F \rrbracket \cup \llbracket G \rrbracket$ • $\llbracket F \land G \rrbracket = \llbracket F \rrbracket \cap \llbracket G \rrbracket$ • $\llbracket (a)F \rrbracket = \langle \cdot a \cdot \rangle \llbracket F \rrbracket$ • $\llbracket (a]F \rrbracket = [\cdot a \cdot ] \llbracket F \rrbracket$ where $\langle \cdot a \cdot \rangle, [\cdot a \cdot] : 2^{(Proc)} \to 2^{(Proc)}$ are defined by $\langle \cdot a \cdot \rangle S = \{ p \in Proc \mid \exists p'. p \xrightarrow{a} p' \text{ and } p' \in S \}$ $\llbracket \cdot a \cdot ] S = \{ p \in Proc \mid \forall p'. p \xrightarrow{a} p' \implies p' \in S \}.$	TheoremLet (Proc, Act, $\{\stackrel{a}{\longrightarrow}   a \in Act\}$ ) be an LTS, $p \in Proc$ and $F$ a formula of Hennessy-Milner logic. Then $p \models F$ if and only if $p \in \llbracket F \rrbracket$ .Proof: by structural induction on the structure of the formula $F$ .
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Image-Finite System         Let $(Proc, Act, \{\stackrel{a}{\longrightarrow}   a \in Act\})$ be an LTS. We call it image-finite iff for every $p \in Proc$ and every $a \in Act$ the set $\{p' \in Proc \mid p \stackrel{a}{\longrightarrow} p'\}$ is finite.	Theorem (Hennessy-Milner)Let (Proc, Act, $\{ \xrightarrow{a}   a \in Act \}$ ) be an image-finite LTS and $p, q \in St$ . Then $p \sim q$ if and only iffor every HM formula $F$ : $(p \models F \iff q \models F)$ .	<pre>hm.cwb agent S = a.S1; agent S1 = b.0 + c.0; agent T = a.T1 + a.T2; agent T1 = b.0; agent T2 = c.0; </pre> <pre>&gt; input "hm.cwb"; &gt; print; &gt; help logic; &gt; checkprop(S,<a>(<b>T &amp; <c>T) true &gt; checkprop(T,<a>(<b>T &amp; <c>T) false &gt; help dfstrong; &gt; dfstrong(S,T); [a]<b>T</b></c></b></a></c></b></a></pre>	
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