Lectures and Tutorials Exam and Literature Lectures and Tutorials Exam and Literature Focus of the Course Overview of the Course Semantics and Verification 2005 • Transition systems and CCS. • Study of mathematical models for the formal description and • Strong and weak bisimilarity, bisimulation games. Lecture 1 analysis of programs. • Hennessy-Milner logic and bisimulation. • Tarski's fixed-point theorem. • Particular focus on parallel and reactive systems. • Hennessy-Milner logic with recursively defined formulae. Timed automata and their semantics. Lecturer: Jiri Srba B2-203. srba@cs.aau.dk • Verification tools and implementation techniques underlying Assistant: Bjørn Haagensen B2-205, bh@cs.aau.dk them. • Binary decision diagrams and their use in verification. • Two mini projects. Organization of the Course Organization of the Course Organization of the Course Lectures and Tutorials Lectures and Tutorials Mini Projects **Tutorials** Lectures • Regularly before each lecture. • Two guest lectures (G. Behrmann, K. G. Larsen). • Verification of a communication protocol in CWB. Supervised peer learning. Ask questions. • Verification of an algorithm for mutual exclusion in UPPAAL. • Two classrooms, work in groups of 2 or 3 people. Take your own notes. • Print out the exercise list, bring literature and your notes. • Read the recommended literature as soon as possible after the • Pensum dispensation. • Feedback from teaching assistant on your request. • Star exercises (*) (part of the exam).

Semantics and Verification 2005

Exam	Literature	Hints
 Individual and oral. Preparation time (star exercises). Pensum dispensation. 	 On-line literature. Compendiums (2004 + 2005, 141 kr). Best Reader Competition with award! 	 Check regularly the course web-page. Anonymous feedback form on the course web-page. Attend and actively participate during tutorials. Take your own notes.
Corganization of the Course Organization of the Course Introduction Formal Models for Reactive Systems Introduction to CCS Aims of the Course Reactive Systems Why Do We Need a Theory?	Classical View Lecture 1 Organization of the Course Introduction Formal Models for Reactive Systems Introduction to CCS Semantics and Verification 2005 Aims of the Course Reactive Systems Why Do We Need a Theory?	Corganization of the Course Introduction Formal Models for Reactive Systems Introduction to CCS Reactive Systems Reactive Systems Reactive Systems Reactive Systems Reactive Systems Why Do We Need a Theory?
Present a general theory of reactive systems and its applications. Design. Specification. Verification (possibly automatic and compositional).	Characterization of a Classical Program Program transforms an input into an output. • Denotational semantics: a meaning of a program is a partial function	What about: Operating systems? Communication protocols? Control programs?
 Give the students practice in modelling parallel systems in a formal framework. Give the students skills in analyzing behaviours of reactive systems. Introduce algorithms and tools based on the modelling 	 states → states Nontermination is bad! In case of termination, the result is unique. 	 Control programs? Mobile phones? Vending machines?
formalisms. Lecture 1 Semantics and Verification 2005	Is this all we need? Lecture 1 Semantics and Verification 2005	Lecture 1 Semantics and Verification 2005

Overview Lectures and Tutorials Exam and Literature Organization of the Course Introduction Formal Models for Reactive Systems Introduction to CCS

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Overview Lectures and Tutorials Exam and Literature

Aims of the Course Reactive Systems Do We Need a Theory?

Why Do We Need a Theory?

Why Do We Need a Theory?

Reactive systems

Analysis of Reactive Systems

The Need for a Theory

Characterization of a Reactive System

Reactive System is a system that computes by reacting to stimuli from its environment.

Key Issues:

- communication and interaction
- parallelism

Nontermination is good!

The result (if any) does not have to be unique.

Why Do We Need a Theory?

Questions

- How can we develop (design) a system that "works"?
- How do we analyze (verify) such a system?

Fact of Life

Even short parallel programs may be hard to analyze.

Conclusion

We need formal/systematic methods (tools), otherwise ...

- Intel's Pentium-II bug in floating-point division unit
- Ariane-5 crash due to a conversion of 64-bit real to 16-bit integer
- Mars Pathfinder
- ...

Formal Models for Reactive System

Formal Models for Reactive System

Labelled Transition System

Labelled Transition System

Classical vs. Reactive Computing

How to Model Reactive Systems

Definition

A labelled transition system (LTS) is a triple $(Proc, Act, \{ \stackrel{a}{\longrightarrow} | a \in Act \})$ where

- Proc is a set of states (or processes),
- Act is a set of labels (or actions), and
- for every $a \in Act$, $\stackrel{a}{\longrightarrow} \subseteq Proc \times Proc$ is a binary relation on states called the transition relation.

We will use the infix notation $s \stackrel{a}{\longrightarrow} s'$ meaning that $(s, s') \in \stackrel{a}{\longrightarrow}$.

Sometimes we distinguish the initial (or start) state.

Classical Reactive/Parallel interaction no nontermination undesirable often desirable unique result yes no semantics $states \hookrightarrow states$

Question

What is the most abstract view of a reactive system (process)?

Answer

A process performs an action and becomes another process.

Semantics and Verification 2005 Semantics and Verification 200 Sequencing, Nondeterminism and Parallelism LTS explicitly focuses on interaction. LTS can also describe: sequencing (a; b) • choice (nondeterminism) (a + b)• limited notion of parallelism (by using interleaving) (a|b)

Closures

Let R, R' and R'' be binary relations on a set A.

Symmetric Closure

R' is the symmetric closure of R if and only if

- \bigcirc R' is symmetric, and
- above, i.e., for any relation R'':

if $R \subseteq R''$ and R'' is symmetric, then $R' \subseteq R''$.

Binary Relations Closures

Definition

A binary relation R on a set A is a subset of $A \times A$.

$$R \subseteq A \times A$$

Sometimes we write x R y instead of $(x, y) \in R$.

Properties

- R is reflexive if $(x, x) \in R$ for all $x \in A$
- R is symmetric if $(x, y) \in R$ implies that $(y, x) \in R$ for all $x, y \in A$
- R is transitive if $(x, y) \in R$ and $(y, z) \in R$ implies that $(x,z) \in R$ for all $x,y,z \in A$

Let R, R' and R'' be binary relations on a set A.

Reflexive Closure

R' is the reflexive closure of R if and only if

- \bigcirc $R \subseteq R'$.
- \bigcirc R' is reflexive, and
- \odot R' is the *smallest* relation that satisfies the two conditions above, i.e., for any relation R'': if $R \subseteq R''$ and R'' is reflexive, then $R' \subseteq R''$.

Labelled Transition Systems – Notation Closures

Let $(Proc, Act, \{\stackrel{a}{\longrightarrow} | a \in Act\})$ be an LTS.

- we extend $\stackrel{a}{\longrightarrow}$ to the elements of Act^*
- $\bullet \longrightarrow = \bigcup_{a \in Act} \xrightarrow{a}$
- ullet is the reflexive and transitive closure of \longrightarrow
- $s \stackrel{a}{\longrightarrow} \text{ and } s \stackrel{a}{\longrightarrow}$
- reachable states

Let R, R' and R'' be binary relations on a set A.

Transitive Closure

R' is the transitive closure of R if and only if

- \bullet $R \subseteq R'$.
- \bigcirc R' is transitive, and
- \circ R' is the *smallest* relation that satisfies the two conditions above, i.e., for any relation R'': if $R \subseteq R''$ and R'' is transitive, then $R' \subseteq R''$.



 P_1 op P_2 \Rightarrow P_1 op P_2

Calculus of Communicating Systems

Process Algebra

Process Algebra

Basic Principle

- Define a few atomic processes (modelling the simplest process behaviour).
- 2 Define compositionally new operations (building more complex process behaviour from simple ones).

Example

- \bullet atomic instruction: assignment (e.g. x:=2 and x:=x+2)
- new operators:
 - sequential composition $(P_1; P_2)$
 - parallel composition $(P_1 \parallel P_2)$

Now e.g. $(x:=1 \parallel x:=2)$; x:=x+2; $(x:=x-1 \parallel x:=x+5)$ is a process.