

# *The $B^{dual}$ – tree:*

## *Indexing Moving Objects by Space Filling Curves in the Dual Space*

By

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# *The $B^{\text{dual}}$ – tree:*

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- Introduction
- Related work
- Problem definition
- The  $B^{\text{dual}}$ -tree
  - Structure and updating
  - Query algorithms
- Experiments
- Conclusions

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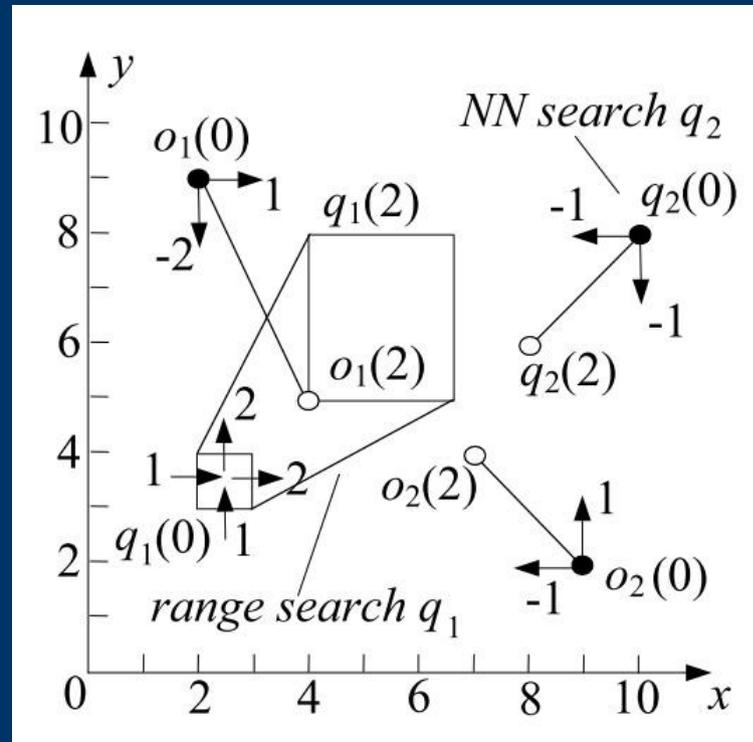
## *Indexing Moving Objects by Space Filling Curves in the Dual Space*

- Introduction:
  - Spatio-temporal objects are spatial objects that change over time.
  - A spatio-temporal database is an index that supports efficient storage and retrieval of information about these objects.
  - Spatio-temporal databases can be divided in two categories:
    - Historical retrieval.
    - Predictive search.

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## Indexing Moving Objects by Space Filling Curves in the Dual Space

- Introduction:
  - Predictive Search
  - Which objects qualify a predicate in the future.



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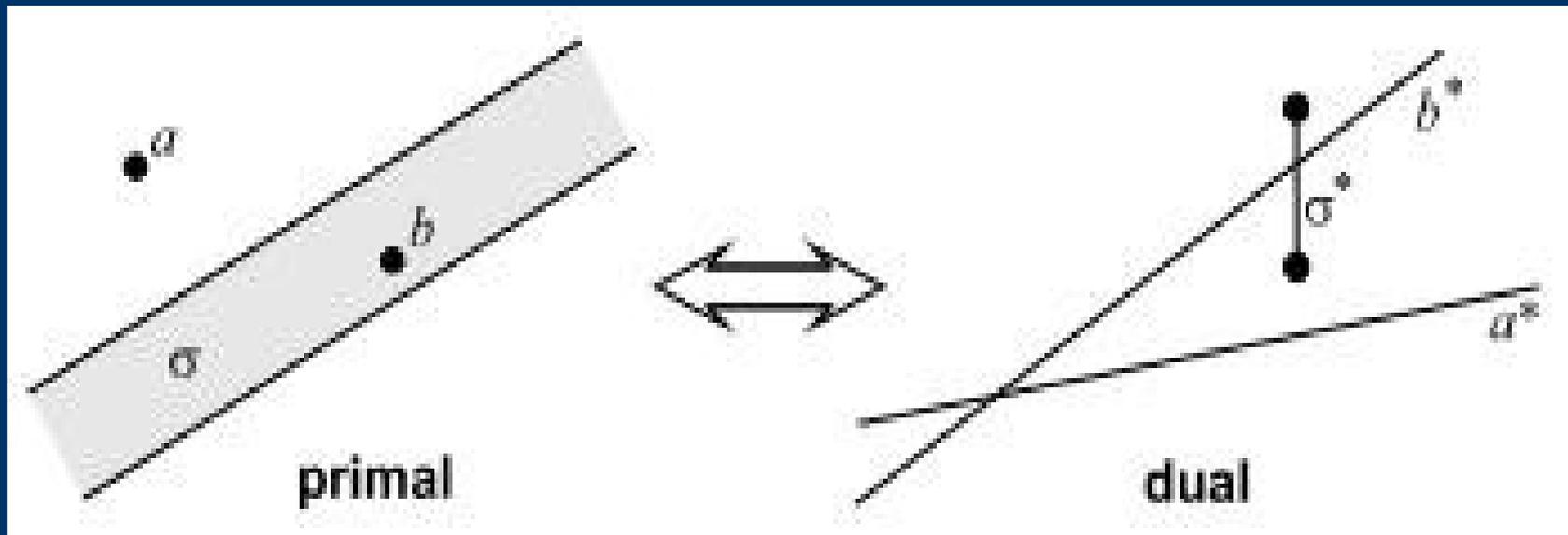
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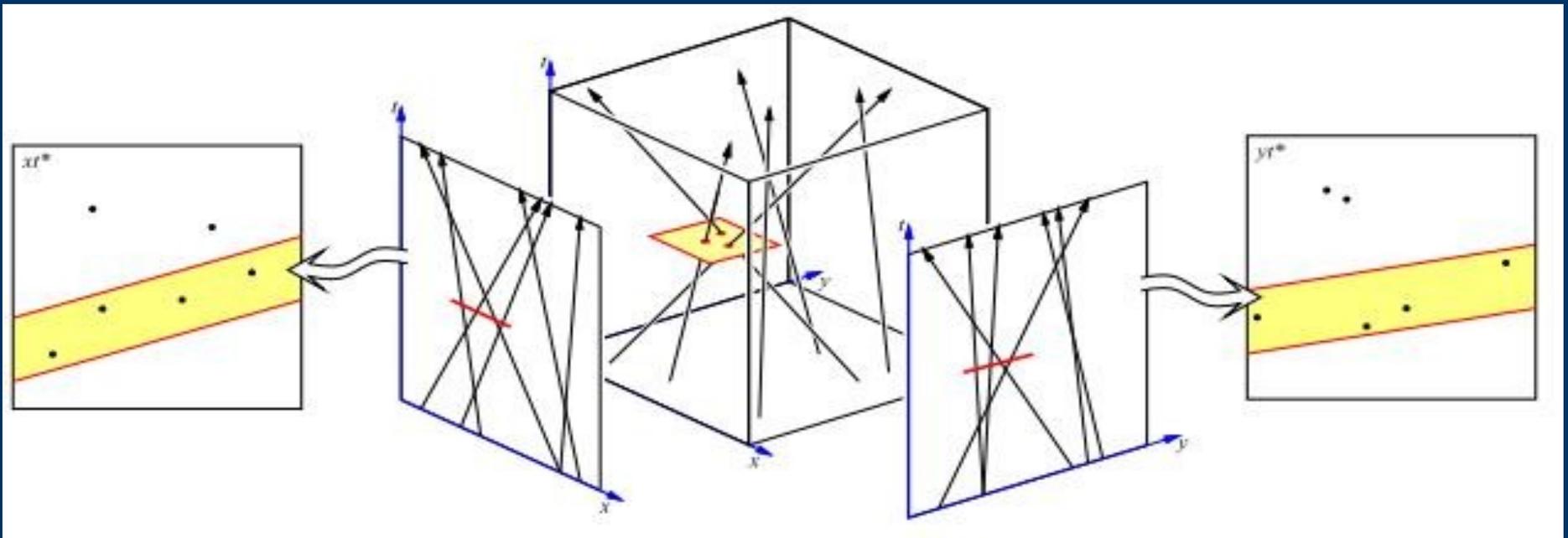
- Related Work: Dual Space Indexing
  - Duality Transformation



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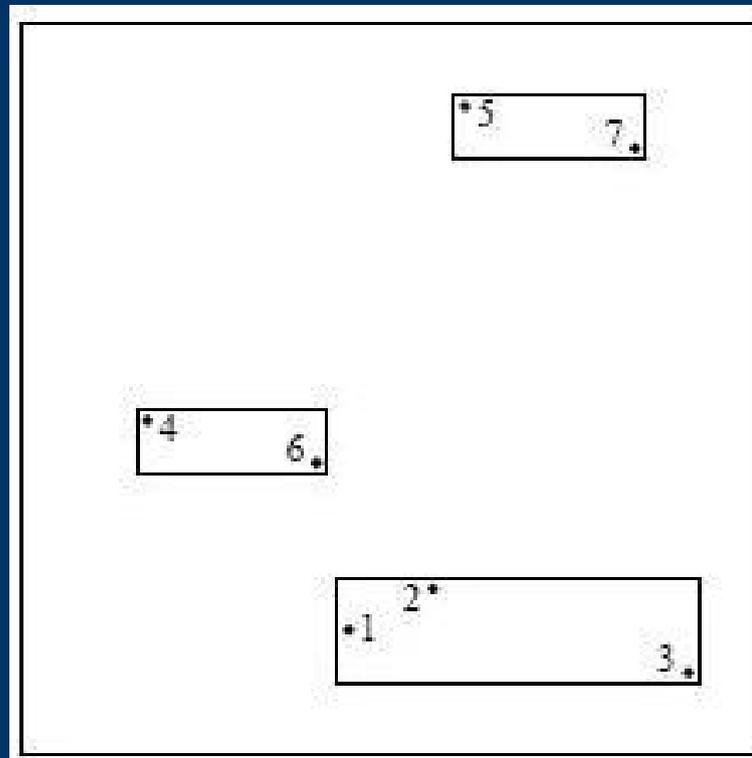
- Related Work: Dual Space Indexing
  - Splits  $(x,y,t)$  into  $(x,x(t)^*)$  and  $(y,y(t)^*)$



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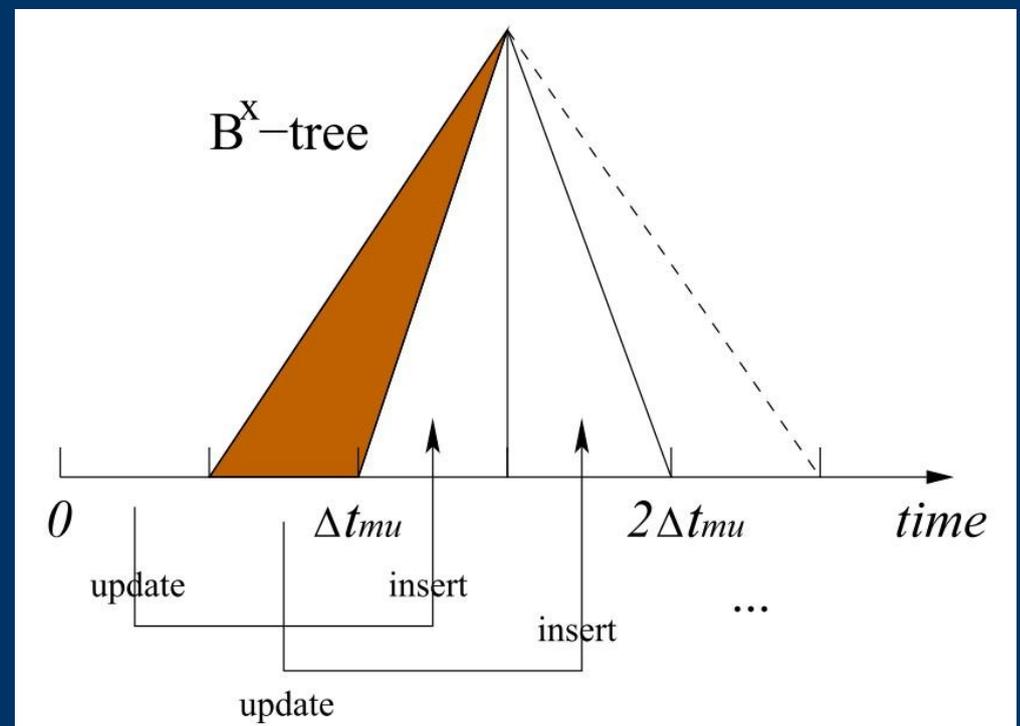
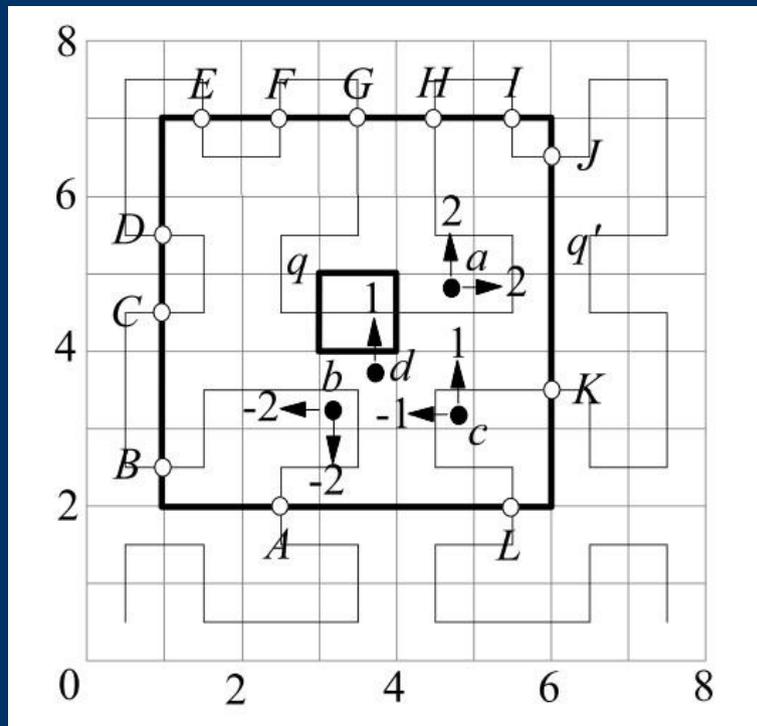
- Related Work: Time-Parameterized R-tree
  - TPR-tree is an R-tree augmented with velocity information to index moving objects.



# The $B^{dual}$ – tree:

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- Related Work:  $B^x$ -tree
  - Uses a space filling curve to index moving objects in  $B^+$ -trees



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# The $B^{dual}$ – tree:

## Indexing Moving Objects by Space Filling Curves in the Dual Space

- Problem definition: moving point
  - A  $d$ -dimensional moving point  $o$  is represented with
    - A reference timestamp  $o.t_{ref}$
    - Its coordinates  $o[1], o[2], \dots, o[d]$  at time  $o.t_{ref}$
    - Its current velocities  $o.v[1], o.v[2], \dots, o.v[d]$

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- Problem definition: MOR
  - A  $d$ -dimensional moving rectangle (MOR)  $r$  is captured by
    - A reference timestamp  $r.t_{ref}$
    - A spatial box (SBox), a  $2d$ -dimensional vector
    - A velocity box (VBox), a  $2d$ -dimensional vector

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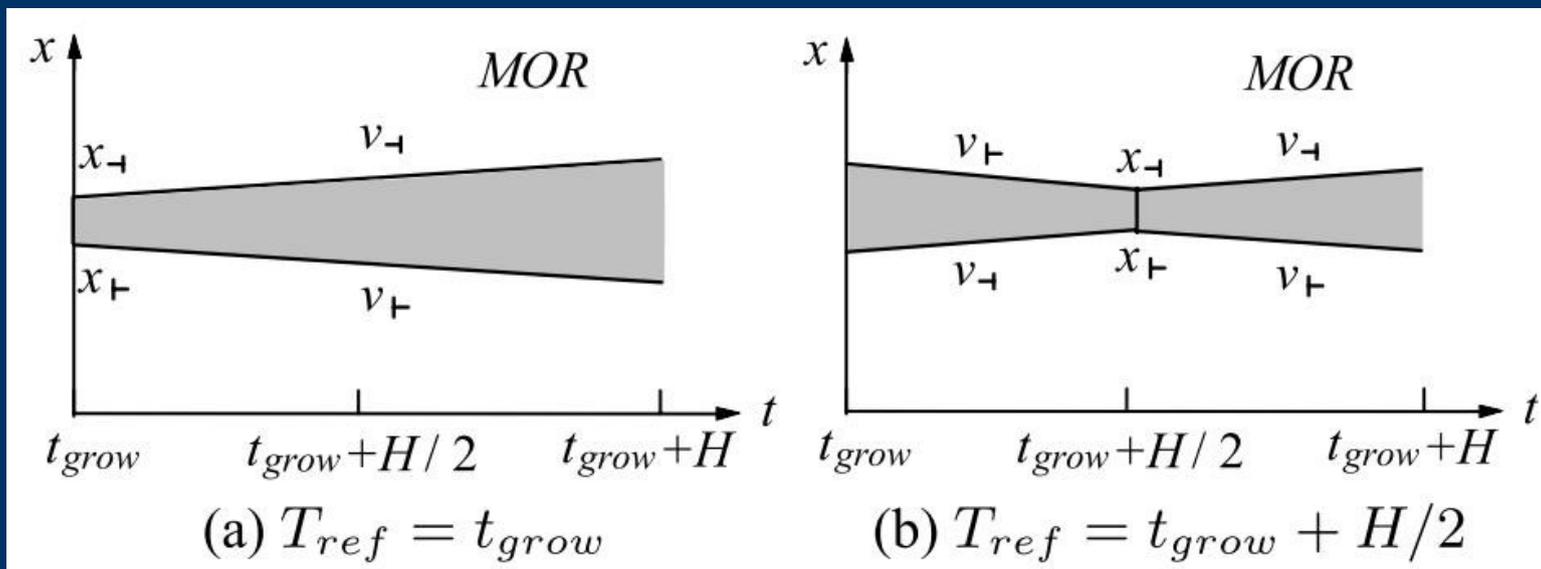
## *Indexing Moving Objects by Space Filling Curves in the Dual Space*

- Motivation
- Related work
- Problem definition
- **The  $B^{\text{dual}}$ -tree**
  - Structure and updating
  - Query algorithms
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# The $B^{\text{dual}}$ – tree:

## Indexing Moving Objects by Space Filling Curves in the Dual Space

- The  $B^{\text{dual}}$ -tree: Structure and updating
  - Two parameters:
    - Horizon  $H$ , the farthest future time that can be efficiently queried.
    - Reference time  $T_{\text{ref}}$ , the reference time for duality transformation.



# The $B^{dual}$ – tree:

## Indexing Moving Objects by Space Filling Curves in the Dual Space

- The  $B^{dual}$ -tree: Structure and updating
  - Duality Transformation
    - $2d$ -dimensions: for every dimension  $i$  in the original data there is a pair  $(o[i](T_{ref}), o.v[i])$
  - Mapping to 1D
    - Hilbert Space filling curve

1	21	22	25	26	37	38	41	42
	20	23	24	27	36	39	40	43
	19	18	29	28	35	34	45	44
	16	17	30	31	32	33	46	47
	15	12	11	10	53	52	51	48
	14	13	8	9	54	55	50	49
	1	2	7	6	57	56	61	62
0	0	3	4	5	58	59	60	63
								1

# The $B^{\text{dual}}$ – tree:

## Indexing Moving Objects by Space Filling Curves in the Dual Space

- The  $B^{\text{dual}}$ -tree: Structure and updating
  - The  $B^{\text{dual}}$ -tree consists of two identical  $B^+$ -trees  $BT_1$  and  $BT_2$
  - When one of the trees is in a *growing state*, the other is in a *shrinking state*
  - In the *growing state*, objects can both be inserted and deleted from the tree
  - In the *shrinking state* objects can only be deleted from the tree

# The $B^{dual}$ – tree:

## Indexing Moving Objects by Space Filling Curves in the Dual Space

- The  $B^{dual}$ -tree: Query Algorithms
  - Perfect MORs
    - Created by  $2d$ -dimensional square of cells
    - The cells have continuous values
    - Query of range [23, 49]
    - Breaks down into 6 perfect MORs
      - [23, 23]
      - [24, 27]
      - [28, 31]
      - [32, 47]
      - [48, 48]
      - [49, 49]

21	22	25	26	37	38	41	42
20	23	24	27	36	39	40	43
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- The  $B^{dual}$ -tree: Query Algorithms
  - The perfect MORs translate into subtrees in the  $B^{dual}$ -tree
  - Each childnode of a subtree is checked to see if it intersects the query range
    - If not it is pruned from the result
    - Else its children are checked for intersection with the query area
  - In this manner the tree is recursively checked until the leafs are encountered

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- Experiments:
  - Experimental data space is two-dimensional
  - Each dimension has a domain of  $[0, 1000]$
  - Objects simulate aircraft travelling between airports.
  - Time horizon of 50 time units.
  - Query cost is measured by averaging over a workload of 100 queries, issued at different current times as the index runs.

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- Experiments:
  - 31 experiments are performed in the categories of Space requirements, Update performance and Query performance
  - In all experiments  $B^{dual}$ -tree performed significantly better than the worst index and in most cases only slightly worse than the best index
  - Conclusion of the article is that the  $B^{dual}$ -tree is superior to the other indexes

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- **Conclusions: Our Project**
  - Deals with indexing of moving objects
  - Duality transformation.
  - Was implemented on disk, whereas our project focuses on main memory.
  - Might be implemented for performance studies
  - Overall conclusion: Highly relevant to our project

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- **Conclusions: Pros**
  - Good illustrations in the beginning of the article showing the problem definition and related work
  - Good introduction, motivation and related work sections.
  - Experimental evidence of performance.

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- Conclusions: Cons
  - Confusing shorthand writing style in article:  
$$x(y) = 2(3)$$
  - A lot of inline math
  - Information is very compressed.
  - Lack of illustration in the part of the article describing the  $B^{\text{dual}}$ -tree itself.