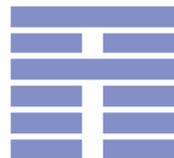


# Modeling & Verification

*Of Real-Time Systems  
using UPPAAL*

**Kim G Larsen**



**BRICS**

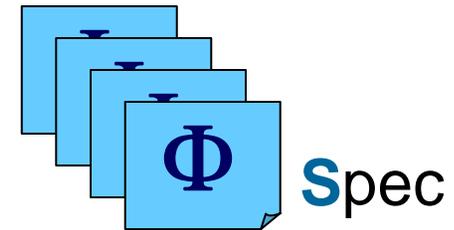
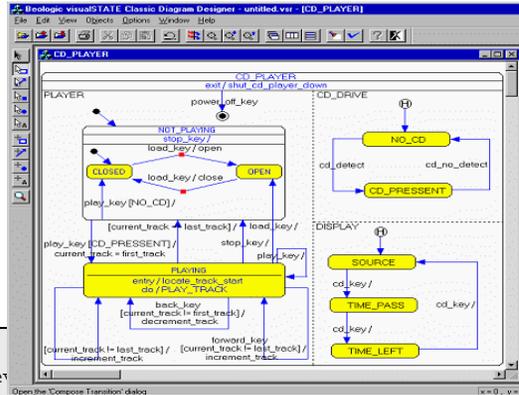
Basic Research  
in Computer Science



CENTER FOR INDLEJREDE SOFTWARE SYSTEMER

# Verifikation og Test

## Model



```

/* Wait for ev
void OS_Wait(void);

/* Operating system visualSTATE process. Mimics a OS process for a
 * visualSTATE system. In this implementation this is the mainloop
 * interfacing to the visualSTATE basic API. */
void OS_VS_Process(void);

/* Define completion code variable. */
unsigned char cc;

void HandleError(unsigned char ccArg)
{
    printf("Error code %c detected, exiting application.\n", ccArg);
    exit(ccArg);
}

/* In d-241 we only use the OS_Wait call. It is used to simulate a
 * system. Its purpose is to generate events. How this is done is up to
 * you.
 */
void OS_Wait(void)
{
    /* Ignore the parameters; just retrieve events from the keyboard and
     * put them into the queue. When EVENT_UNDEFINED is read from the
     * keyboard, return to the calling process. */
    SEM_EVENT_TYPE event;
    int num;

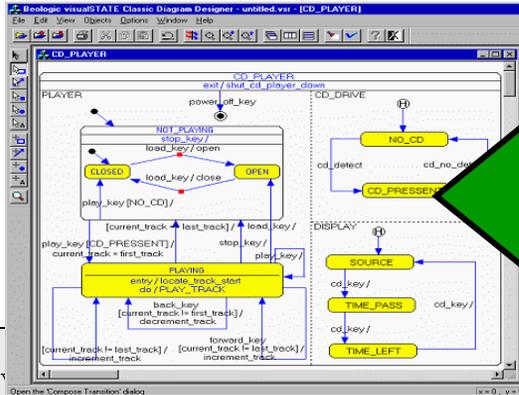
```



System

# Verifikation og Test

Model



```

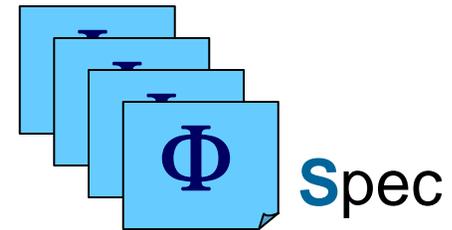
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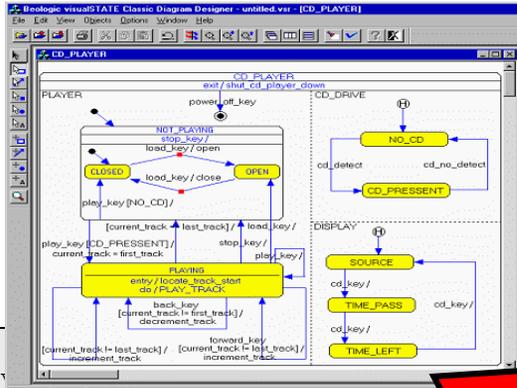
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```



System

# Verifikation og Test

## Model



```

/* Wait for event.
void OS_Wait(void);

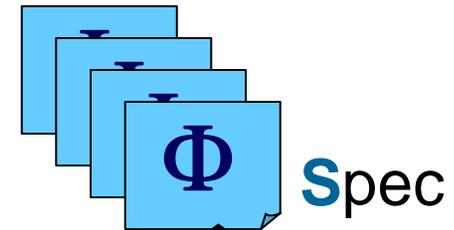
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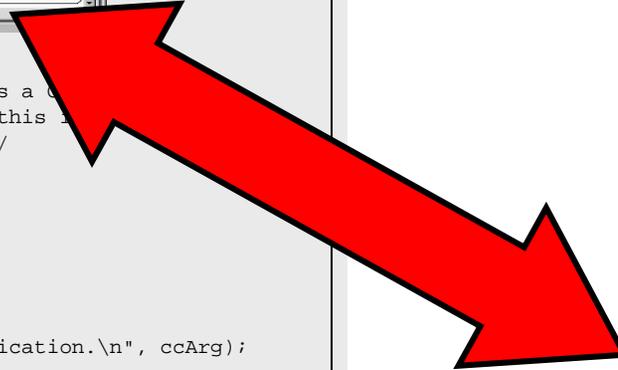
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```



System





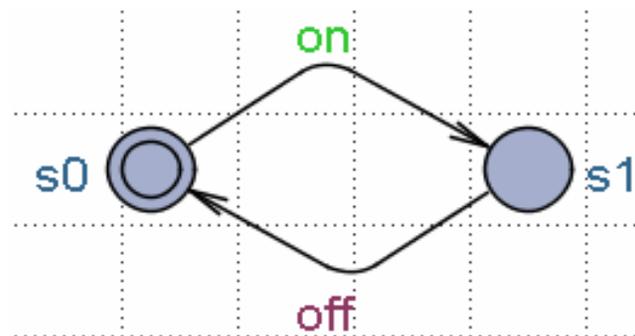
Modelling Behaviour  
using  
State Machines

# Modelling processes

- ❖ A process is the execution of a sequential program.
- ❖ modeled as a finite state machine (LTS)
  - transits from state to state
  - by executing a sequence of *atomic* actions.

a light switch

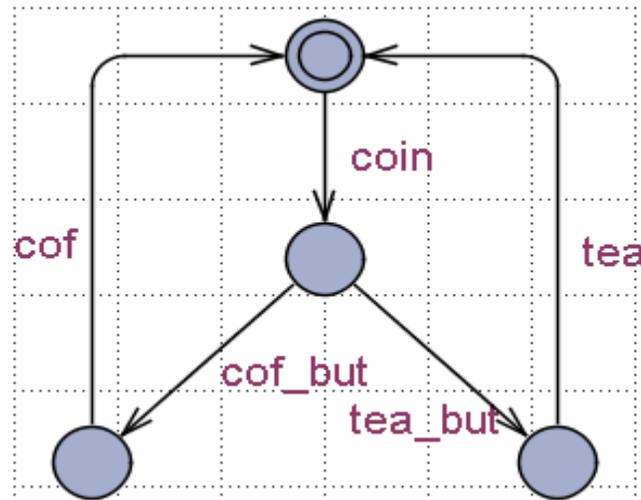
LTS



on → off → on → off → on → off → .....

a sequence of  
actions or *trace*

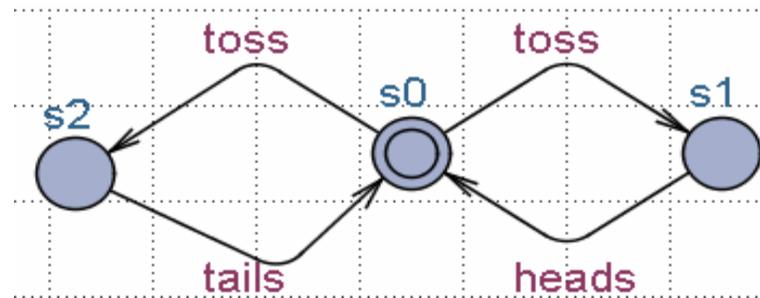
# Modelling Choices



- Who or what makes the choice?
- Is there a difference between input and output actions?

# Non-deterministic Choice

## ❖ Tossing a coin



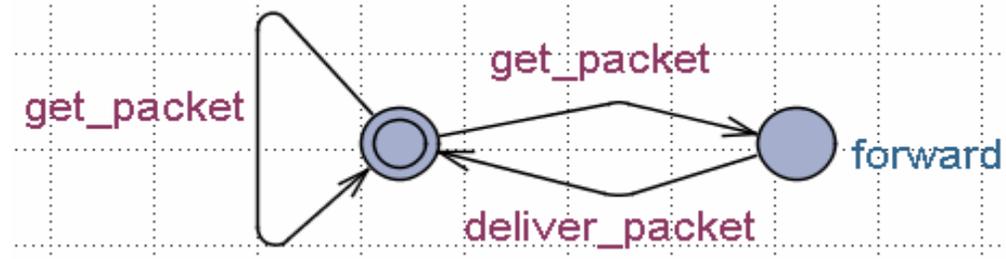
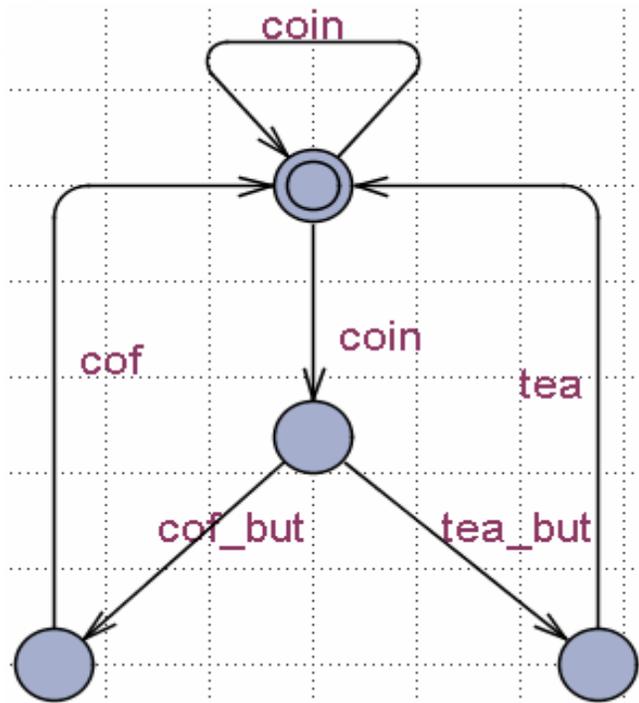
## ❖ Possible traces?

- Both outcomes possible
- Nothing said about relative frequency
- If coin is fair, the outcome is 50/50

# Non-Deterministic Choice modelling failure

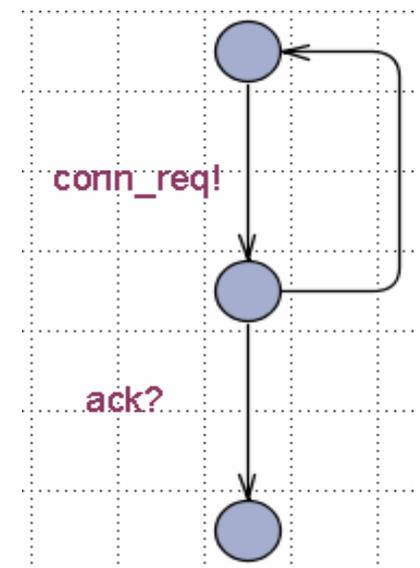
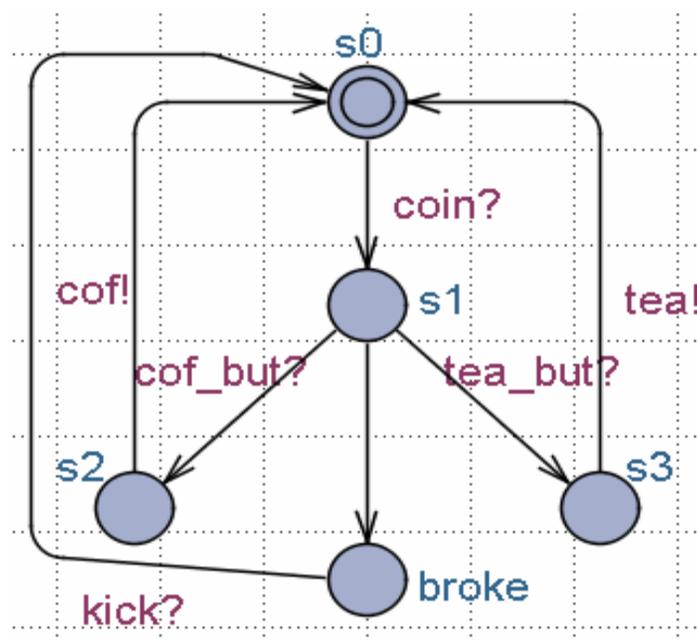
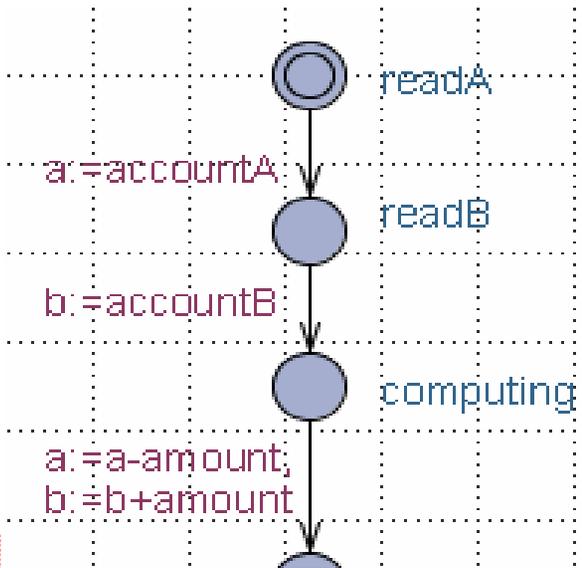
How do we model an unreliable communication channel which accepts **packets**, and if a failure occurs produces no output, otherwise **delivers** the packet to the receiver?

Use non-determinism...

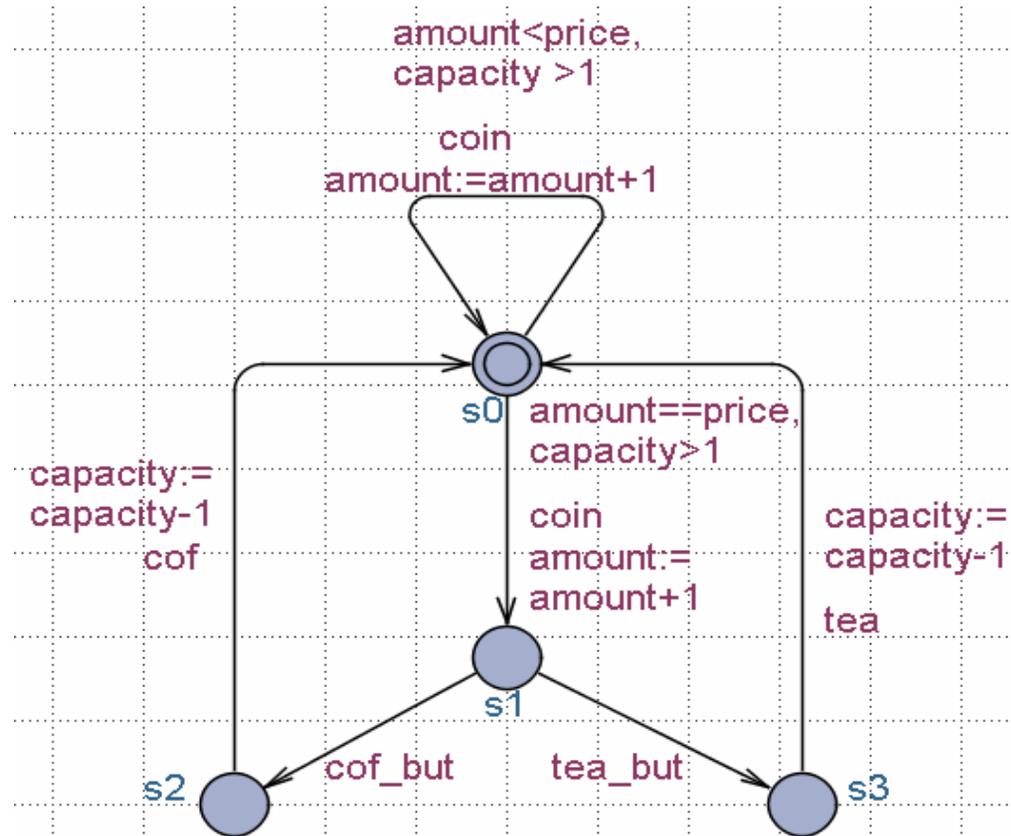


# Internal-Actions

- ❖ Spontaneous actions
- ❖ Internal actions
- ❖ Tau-actions
- ❖ Internal transitions can be taken on the initiative of a single machine without communication with others

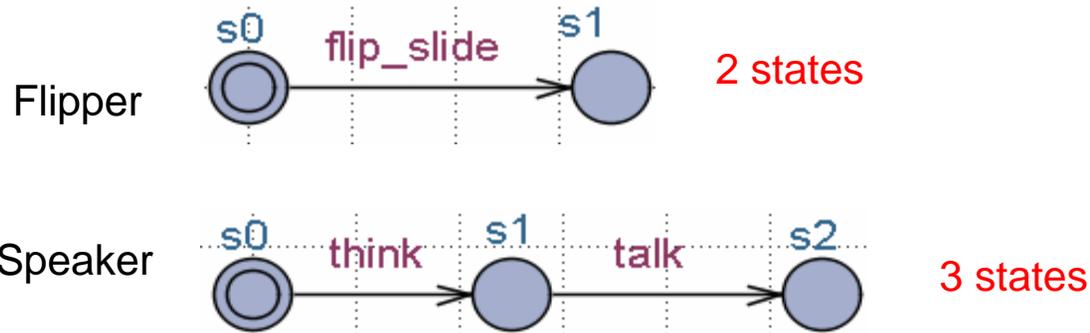


# Extended FSM

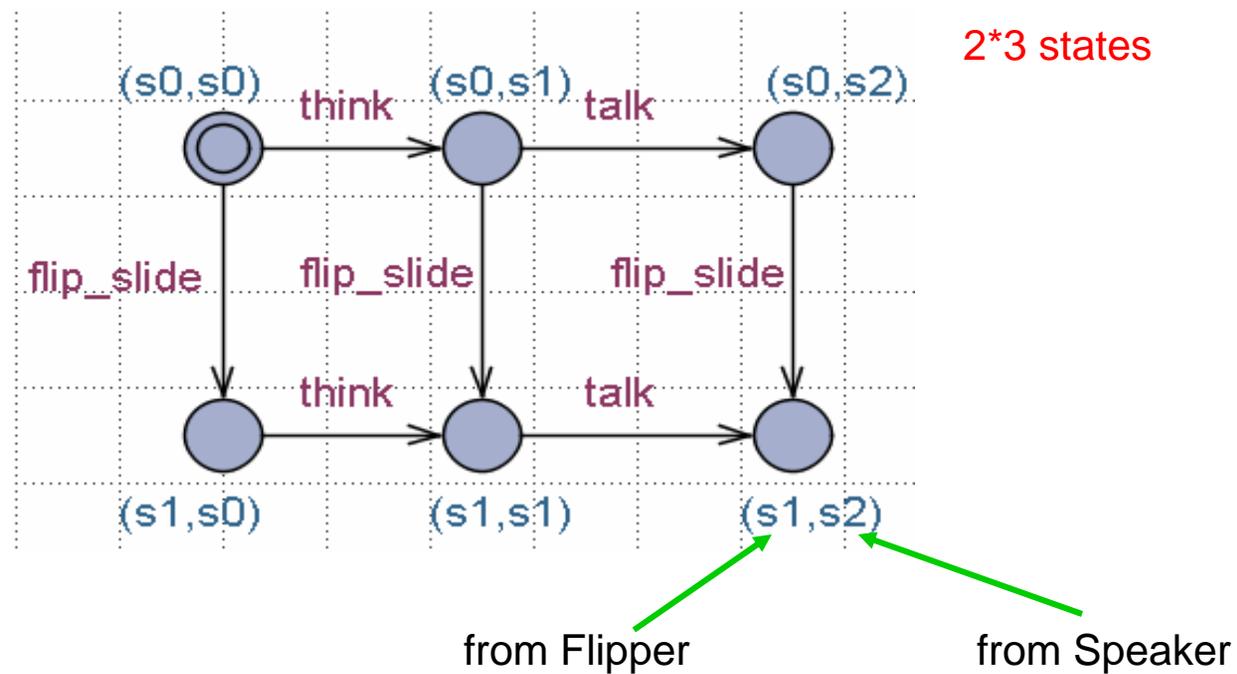


- EFSM = FSM + **variables** + **enabling conditions** + **assignments**
- Transition still atomic
- Can be translated into FSM if variables have bounded domain
- State: control location+variable states: (state,total,capacity)
- (s0,5,10)

# Parallel Composition: interleaving



Lecturer =  
Speaker || Flipper

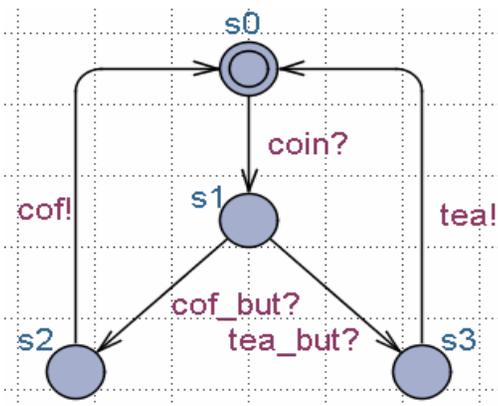


Kim G. Larsen

# Process Interaction

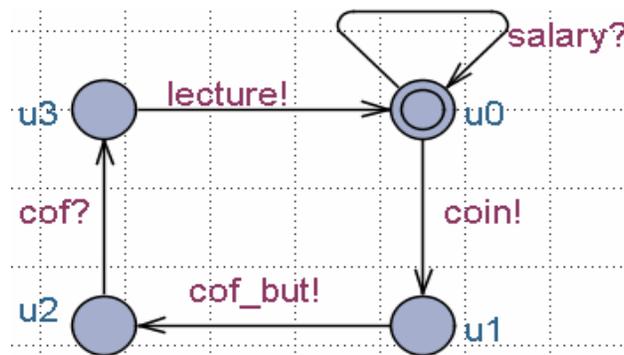
- ❖ ! = Output, ? = Input
- ❖ Handshake communication
- ❖ Two-way

Coffee Machine



4 states

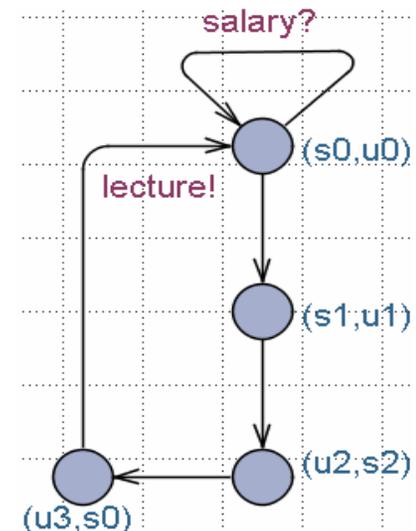
Lecturer



4 states

University =  
Coffee Machine || Lecturer

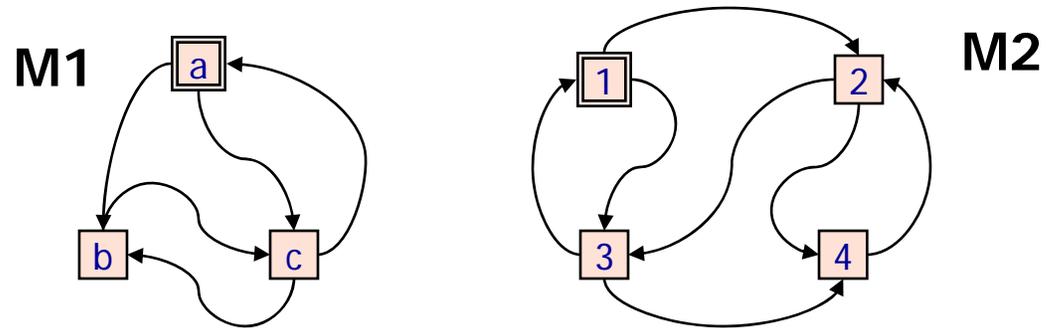
- LTS?
- How many states?
- Traces ?



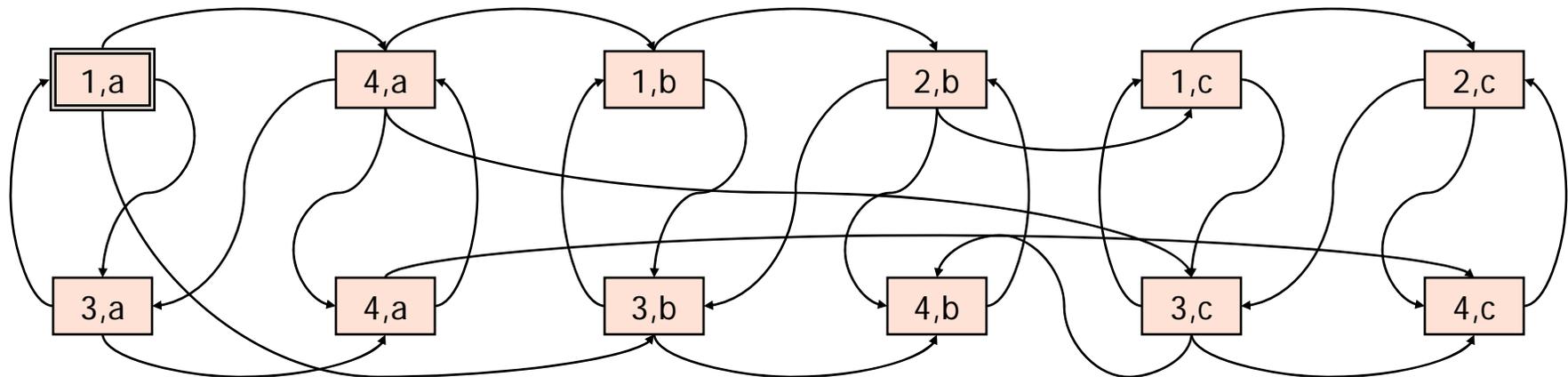
synchronization results in internal actions

4 states: Interaction constrain overall behavior

# Composition



M1 x M2

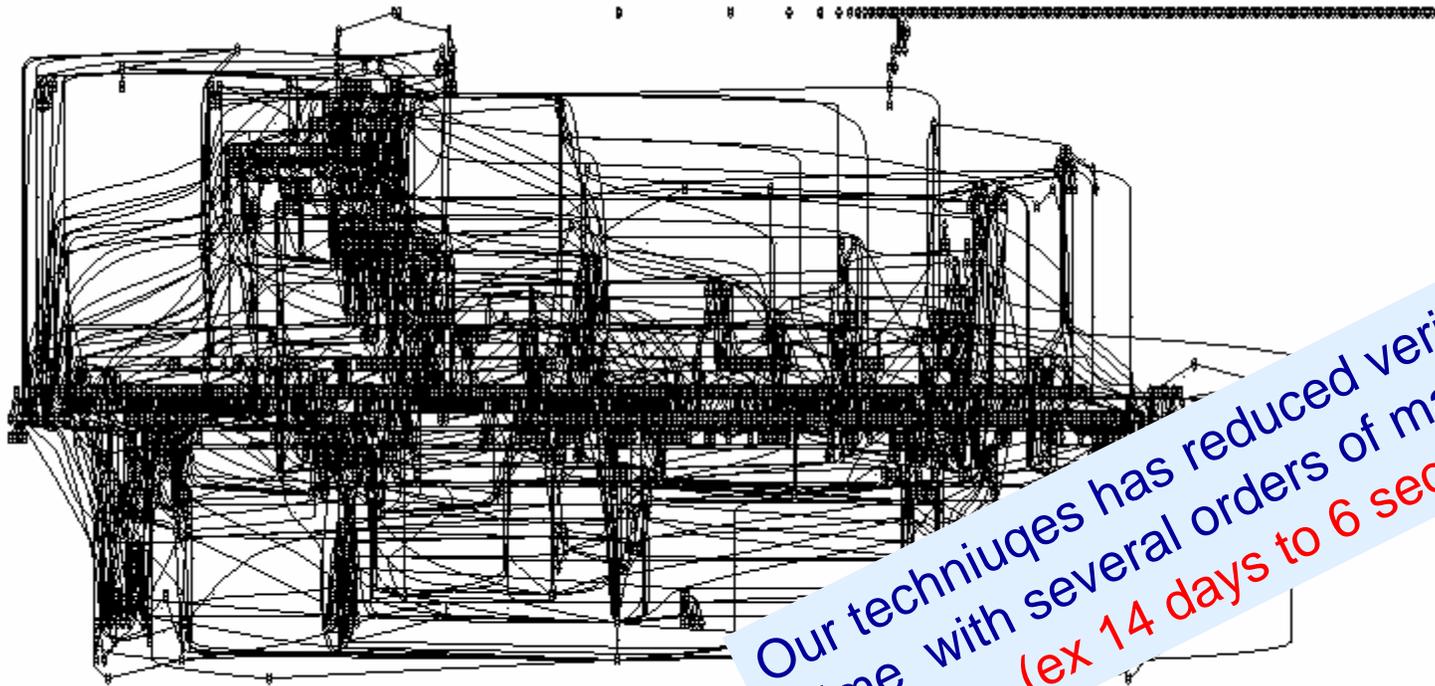


All combinations=  
exponential in no of machines

# Train Simulator

1421 machines  
11102 transitions  
2981 inputs  
2667 outputs  
3204 local states  
Declare state sp.:  $10^{476}$

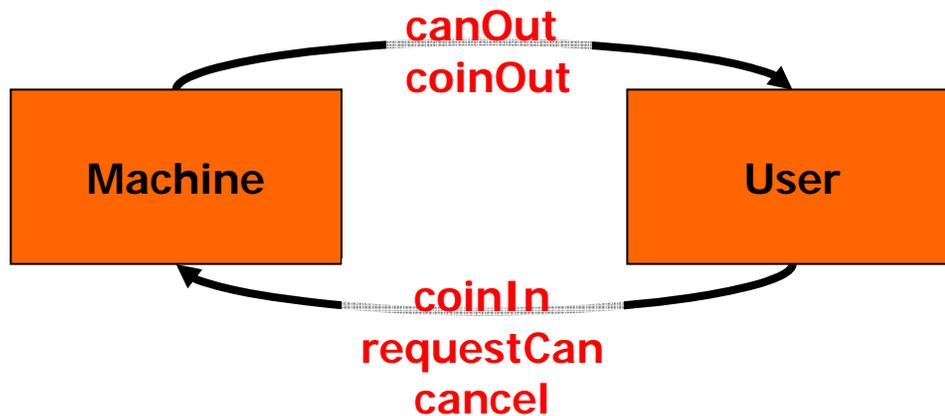
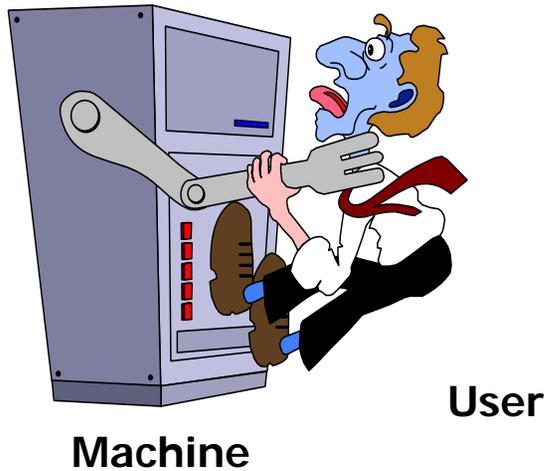
BUGS ?



Our techniques has reduced verification  
time with several orders of magnitude  
(ex 14 days to 6 sec)

# Modelling Exercise

## The Vending Machine



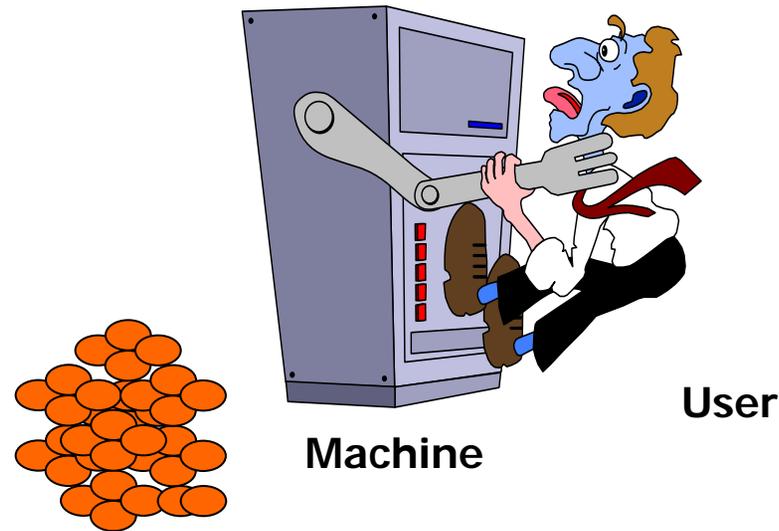
Assumption: 1 can = 1 coin!

- Simulate model w Random User
- Model Fair User
- Model Non-Thirsty User
- Deadlocks ?
  
- Cans requested will be delivered ?
- Cancellations are obeyed ?
  
- What happens if multiple users?

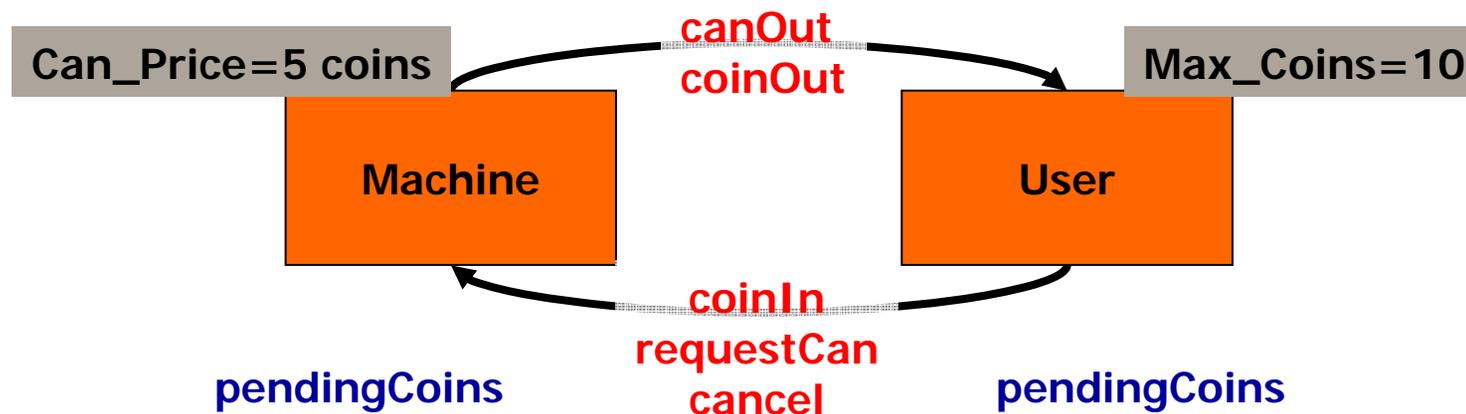
**Exercise**

# Modelling Exercise

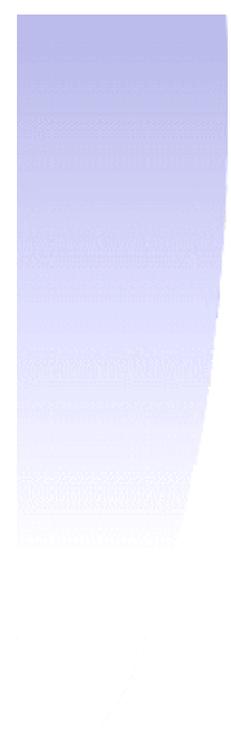
## The Vending Machine



- Extend model of Machine and FairUser
- Do extensive simulation



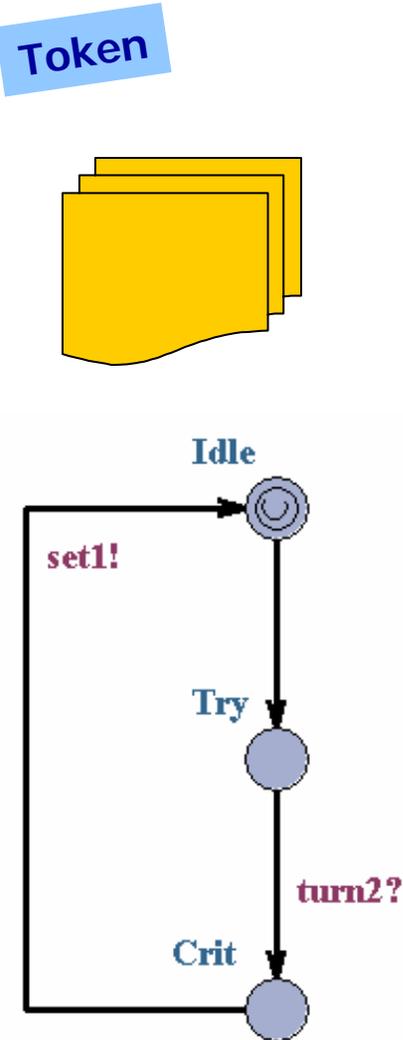
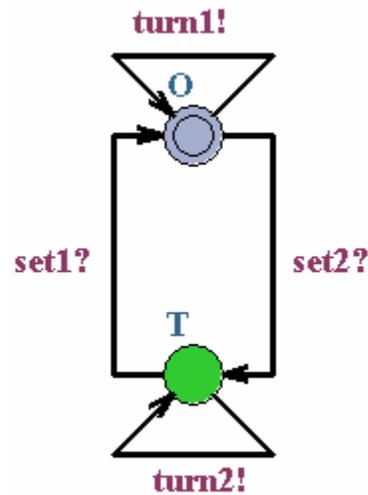
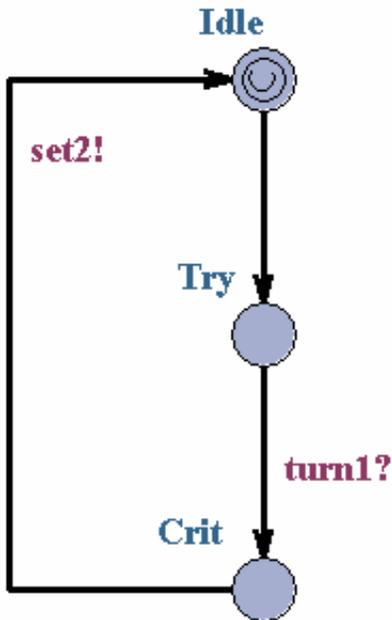
**Exercise**



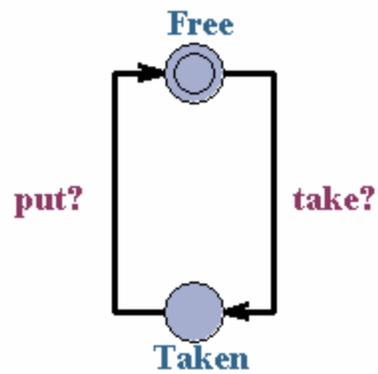
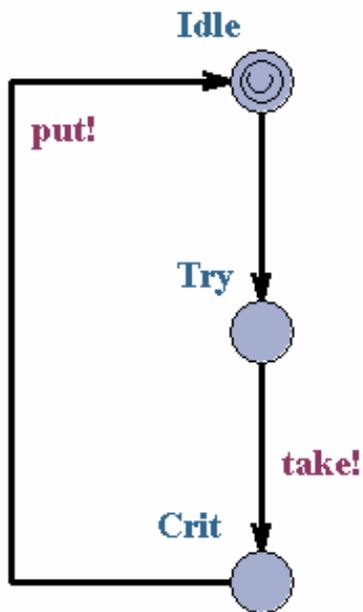
# Verification = Model Checking

- **Reachability**
- **Generic properties**

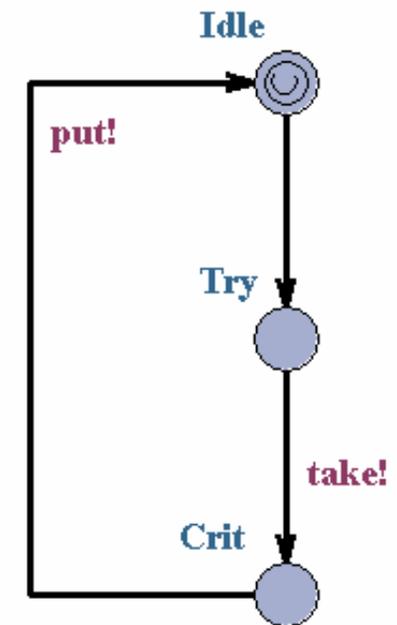
# Mutual Exclusion



# Mutual Exclusion

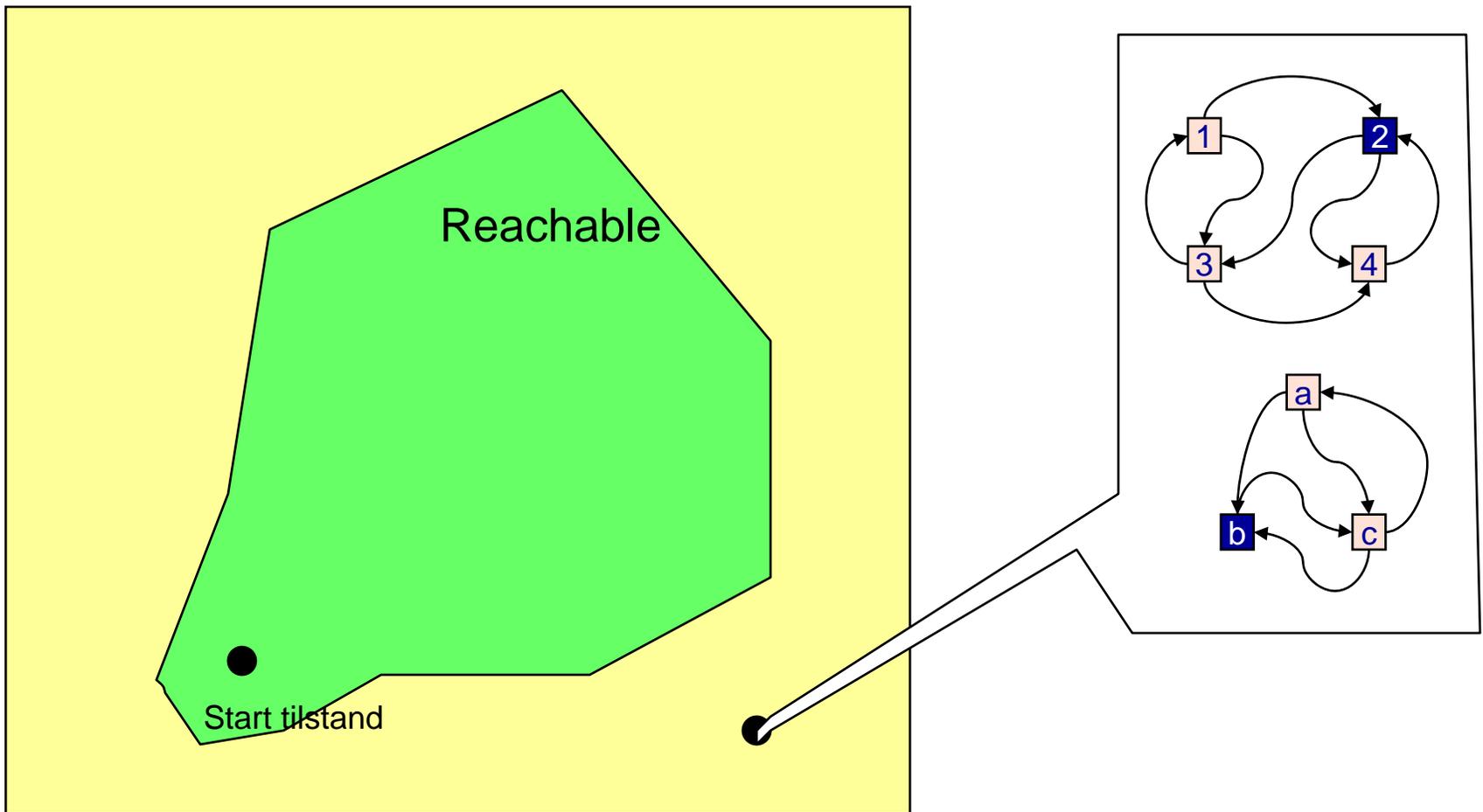


Semafor



# Udforskning af Tilstandsrum

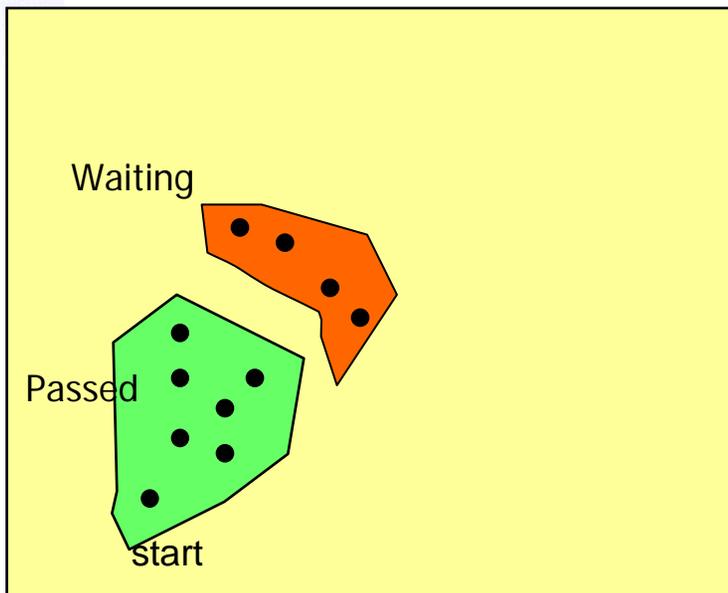
Erklæret tilstandsrum



# Udforskning af tilstandsrum

## Forward Reachability Analysis

Erklæret tilstandsrum



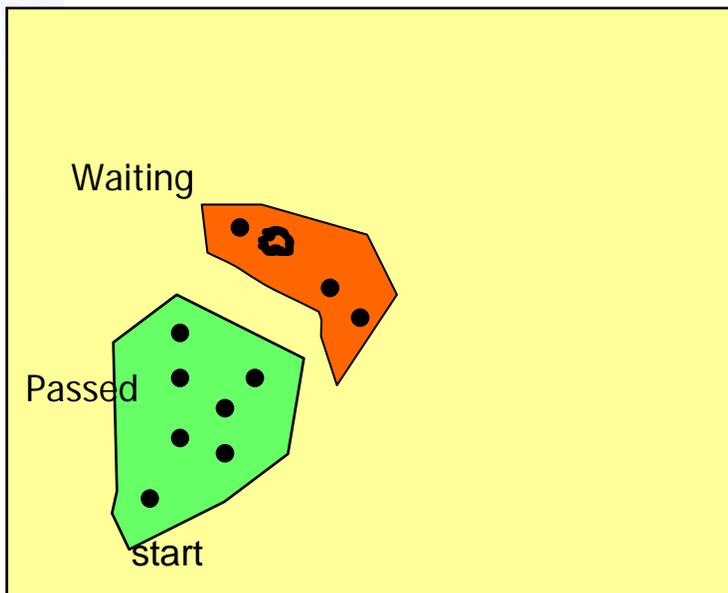
```

Passed := ∅
Waiting := {s0}
While (Waiting ≠ ∅)
  {
    select s ∈ Waiting
    Waiting := Waiting \ {s}
    if s ∉ Passed
      whenever (s → t) then
        Waiting := Waiting ∪ {t}
        Passed := Passed ∪ {s}
  }
  
```

# Udforskning af tilstandsrum

## Forward Reachability Analysis

Erklæret tilstandsrum



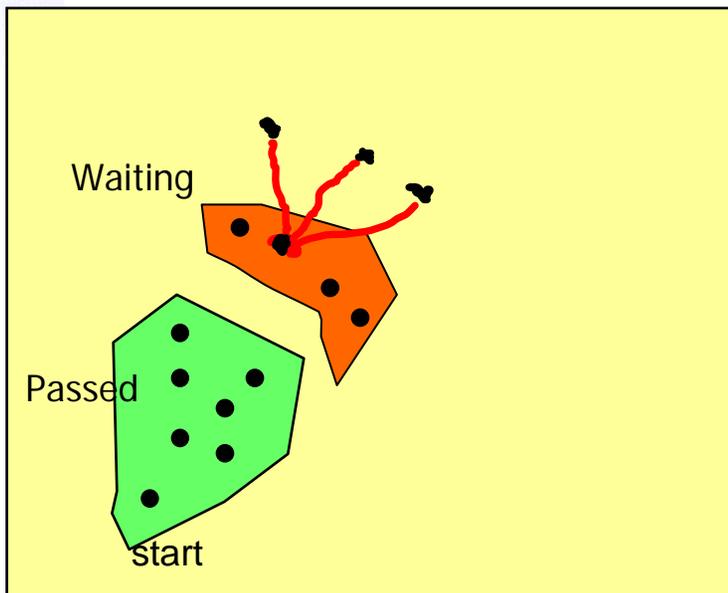
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```

# Udforskning af tilstandsrum

## Forward Reachability Analysis

Erklæret tilstandsrum



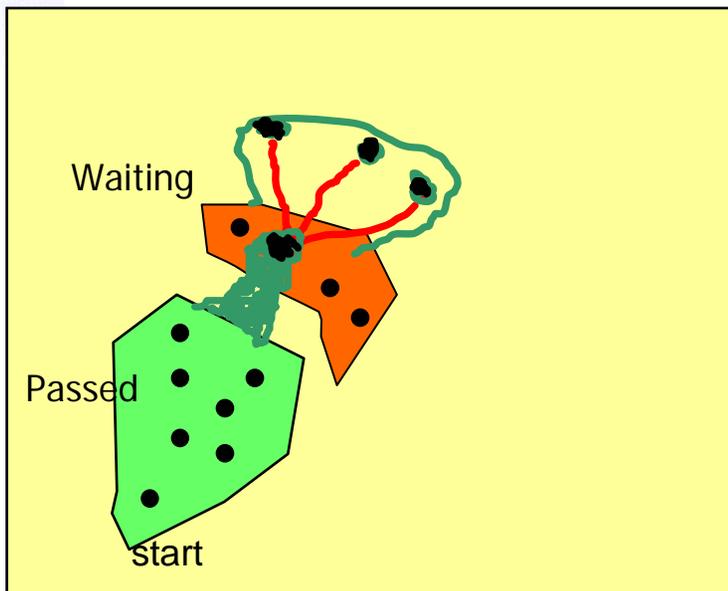
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# Udforskning af tilstandsrum

## Forward Reachability Analysis

Erklæret tilstandsrum

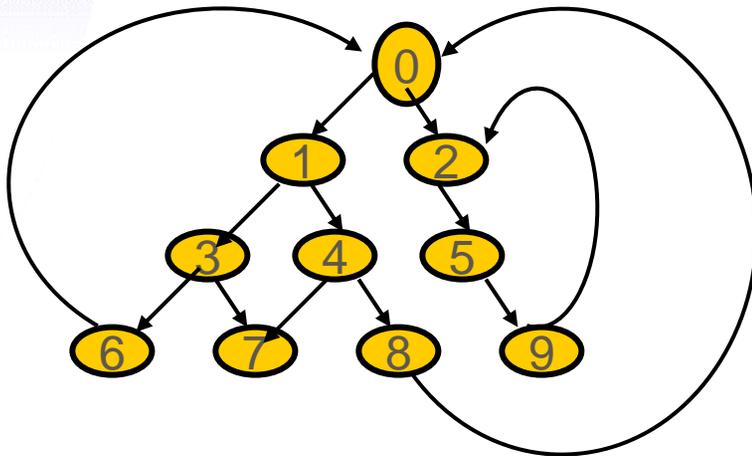


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```

# Udforskning af tilstandrum

## Forward Reachability Analysis



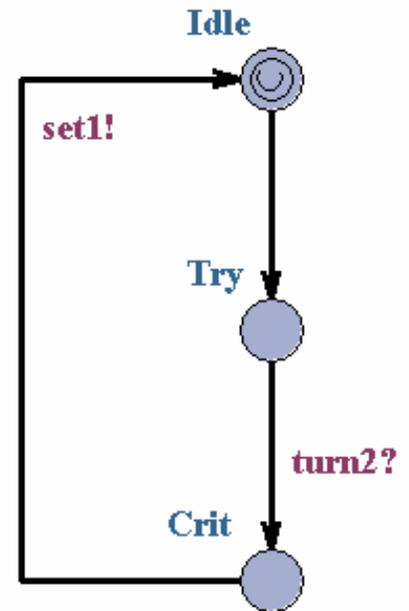
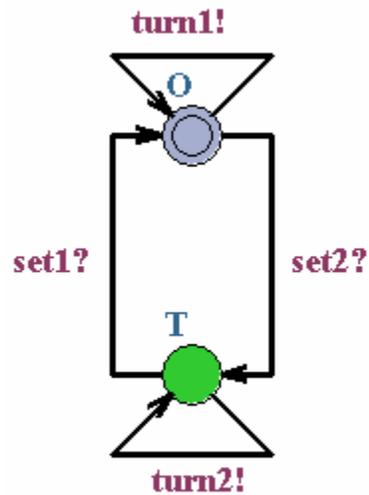
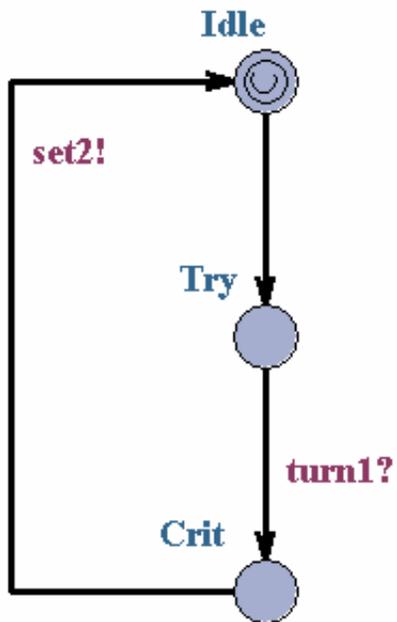
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  whenever (s → t) then
    Waiting := Waiting ∪ {t}
    Passed := Passed ∪ {s}
}
  
```

**Depth-first search:** organize Waiting as a **Stack**  
Order: 0 1 3 6 7 4 8 2 5 9

**Breadth-first search:** organize Waiting as a **Queue**  
Order: 0 1 2 3 4 5 6 7 8 9

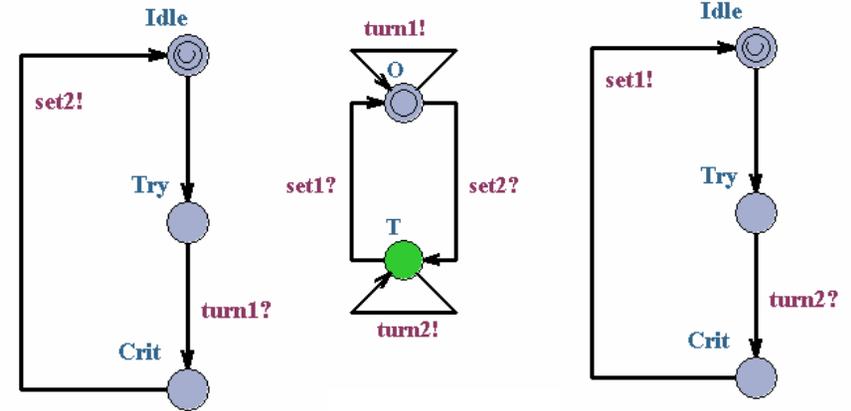
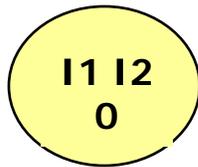
# Gensidig Udelukkelse



Token

# Gensidig udelukkelse

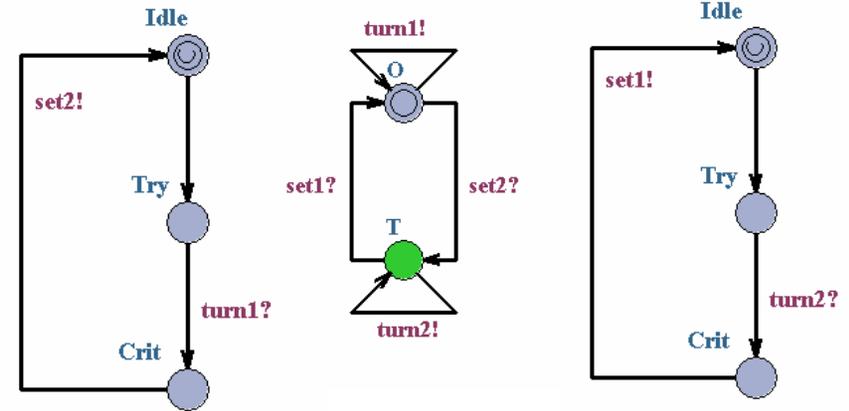
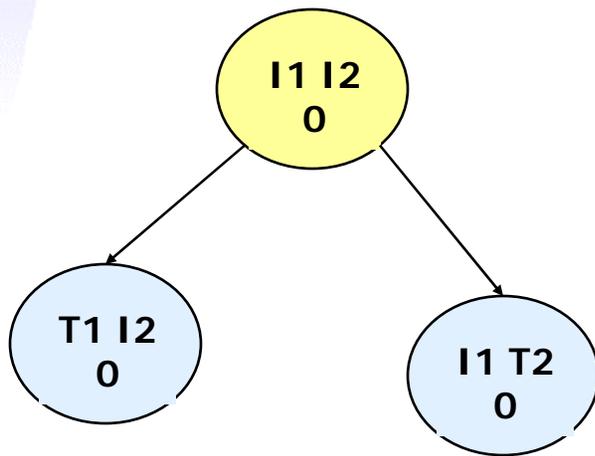
## *Forward Reachability*



Token

# Gensidig udelukkelse

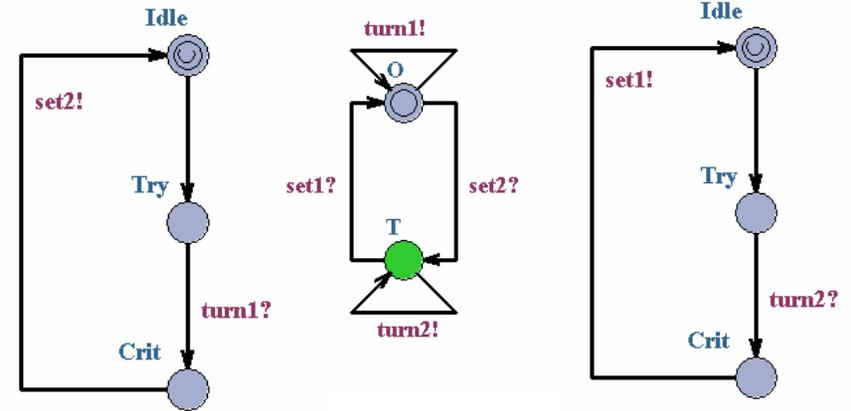
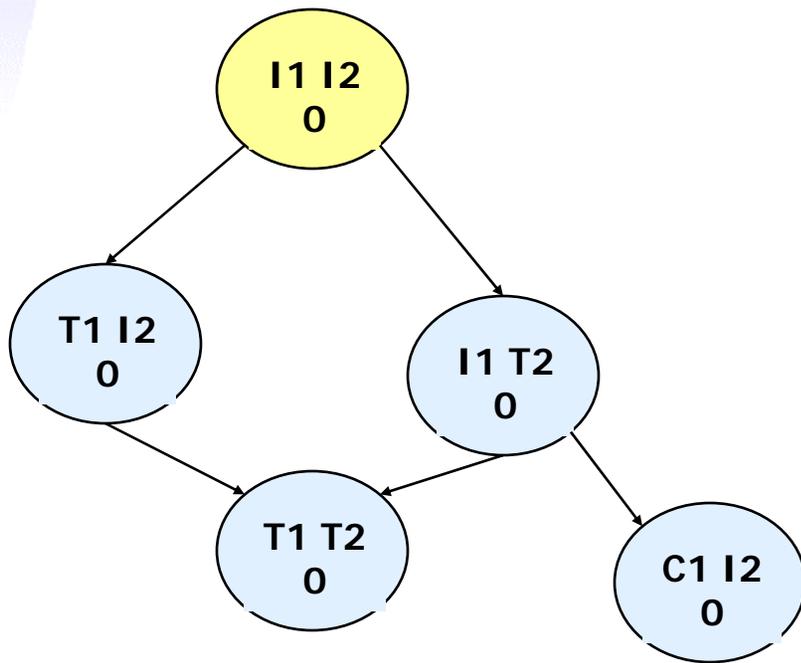
## Forward Reachability



Token

# Gensidig udelukkelse

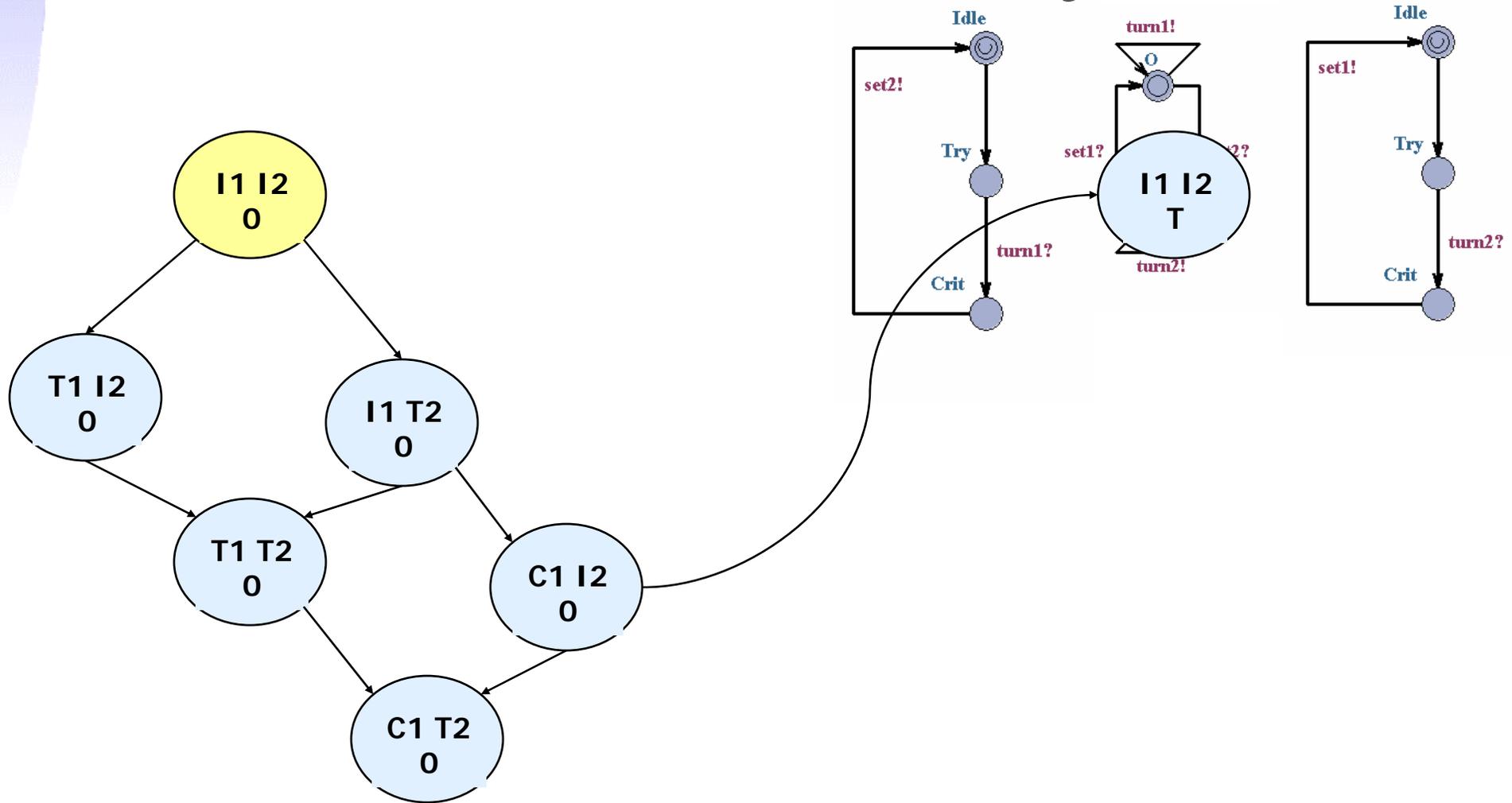
## Forward Reachability



Token

# Gensidig udelukkelse

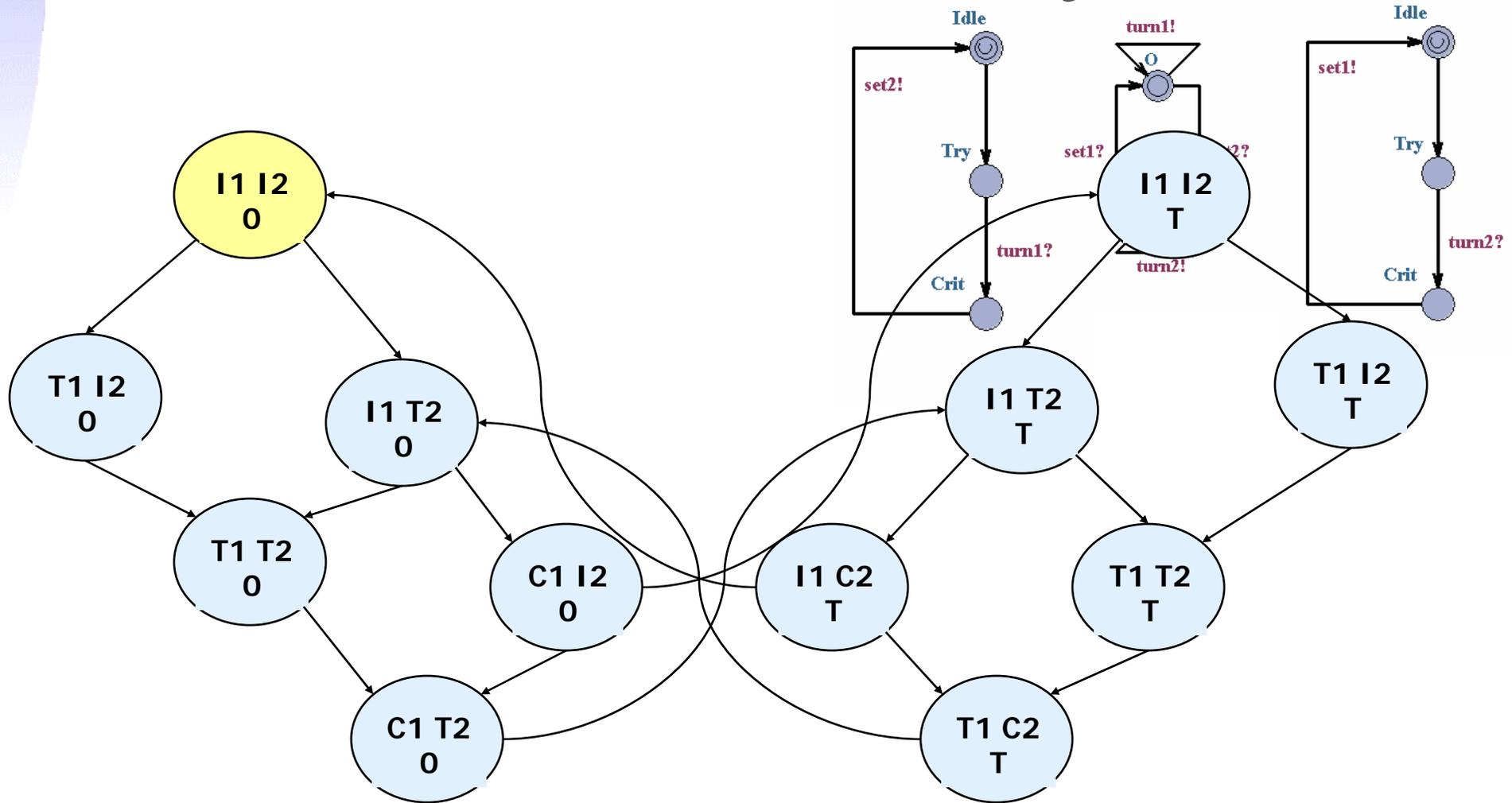
## Forward Reachability



Token

# Gensidig udelukkelse

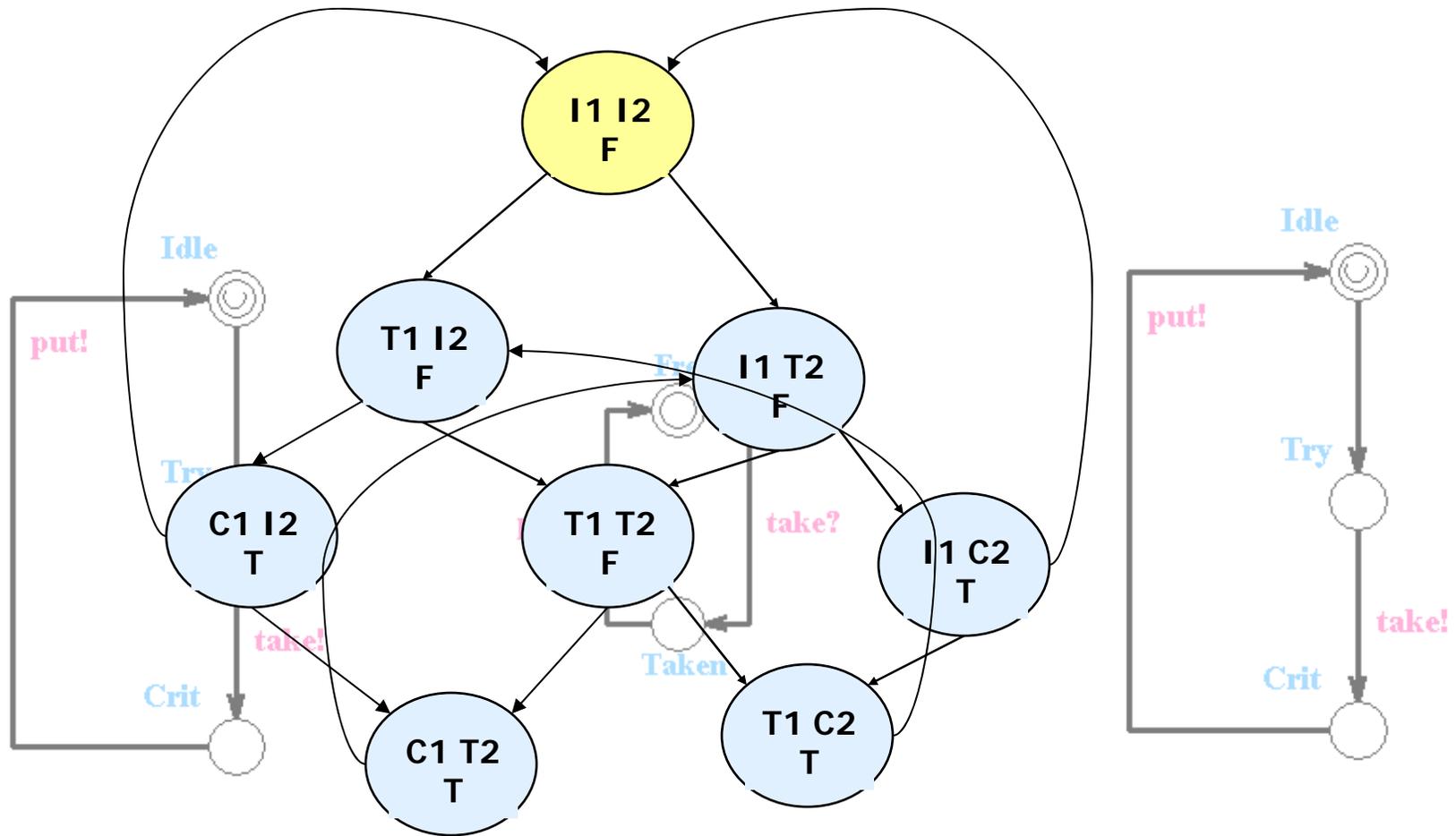
## Forward Reachability



Token

# Gensidig udelukkelse

*Forward Reachability*



Semafor

# Generiske egenskaber

- Non-determinisme
- Tilstande der ikke aktiveres
- Transitioner der ikke bruges
- Input der ikke processeres
- Output der ikke genereres
- Lokal deadlock
- System deadlock

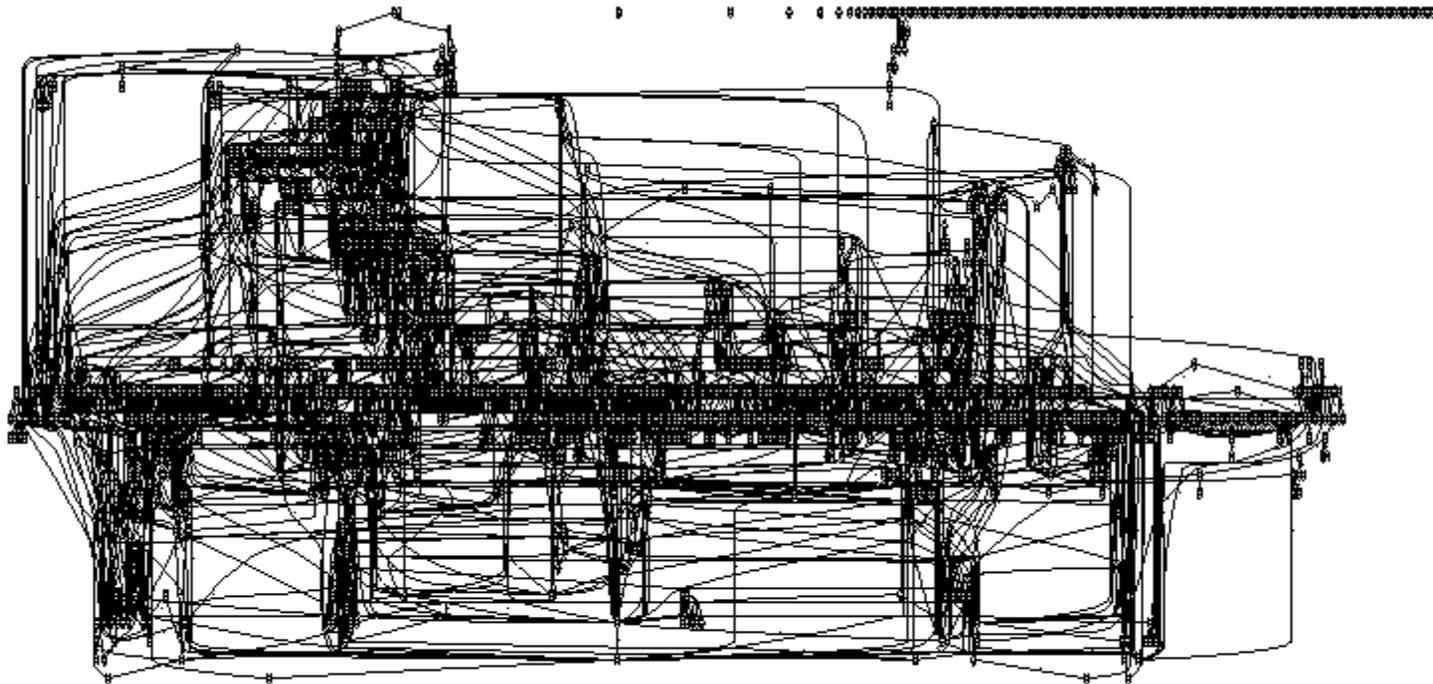
**Kan alle reduceres til  
REACHABILITY**

# Train Simulator

VVS  
visualSTATE

1421 machines  
11102 transitions  
2981 inputs  
2667 outputs  
3204 local states  
Declare state sp.:  $10^{476}$

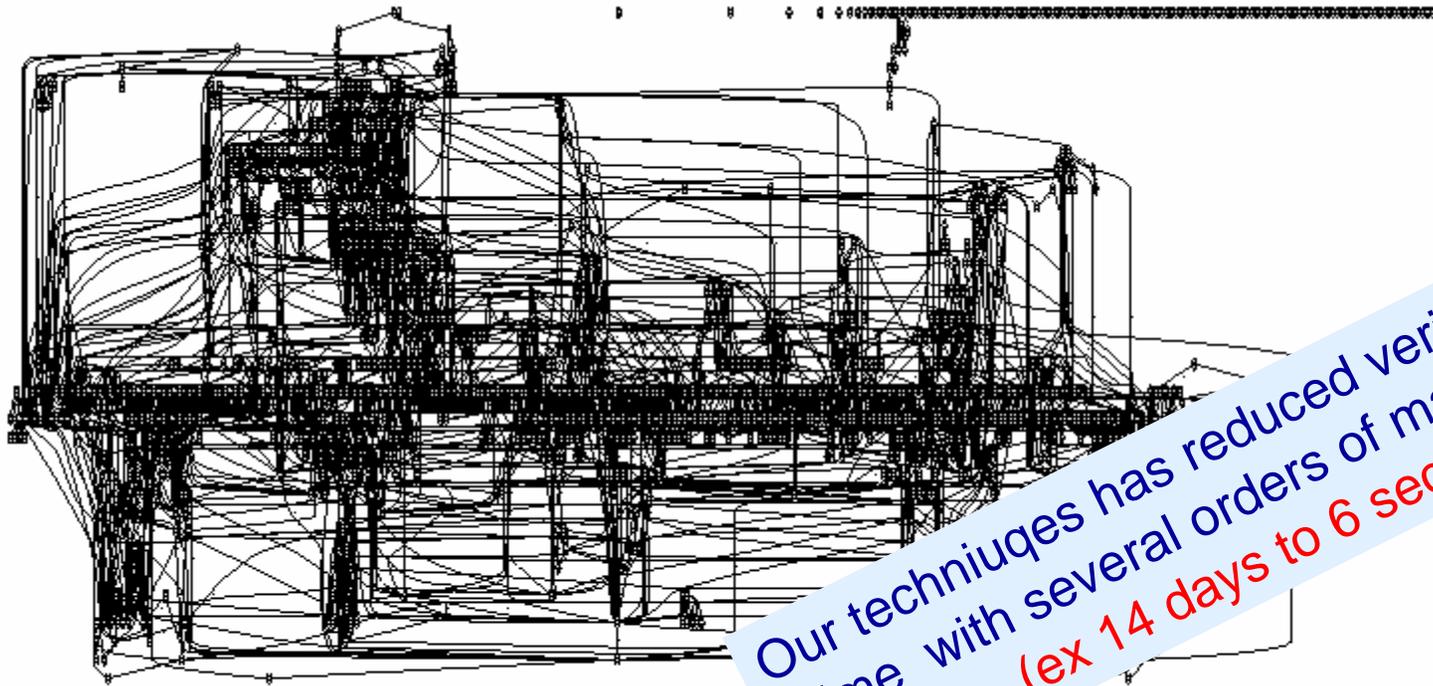
**BUGS ?**



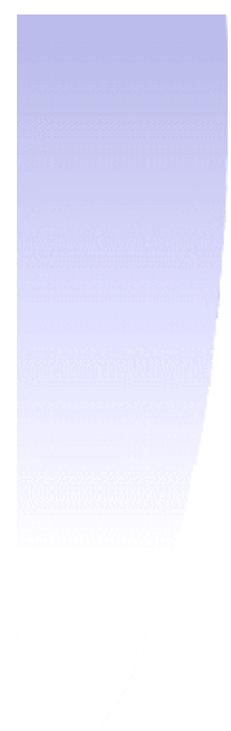
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BUGS ?



Our techniques has reduced verification  
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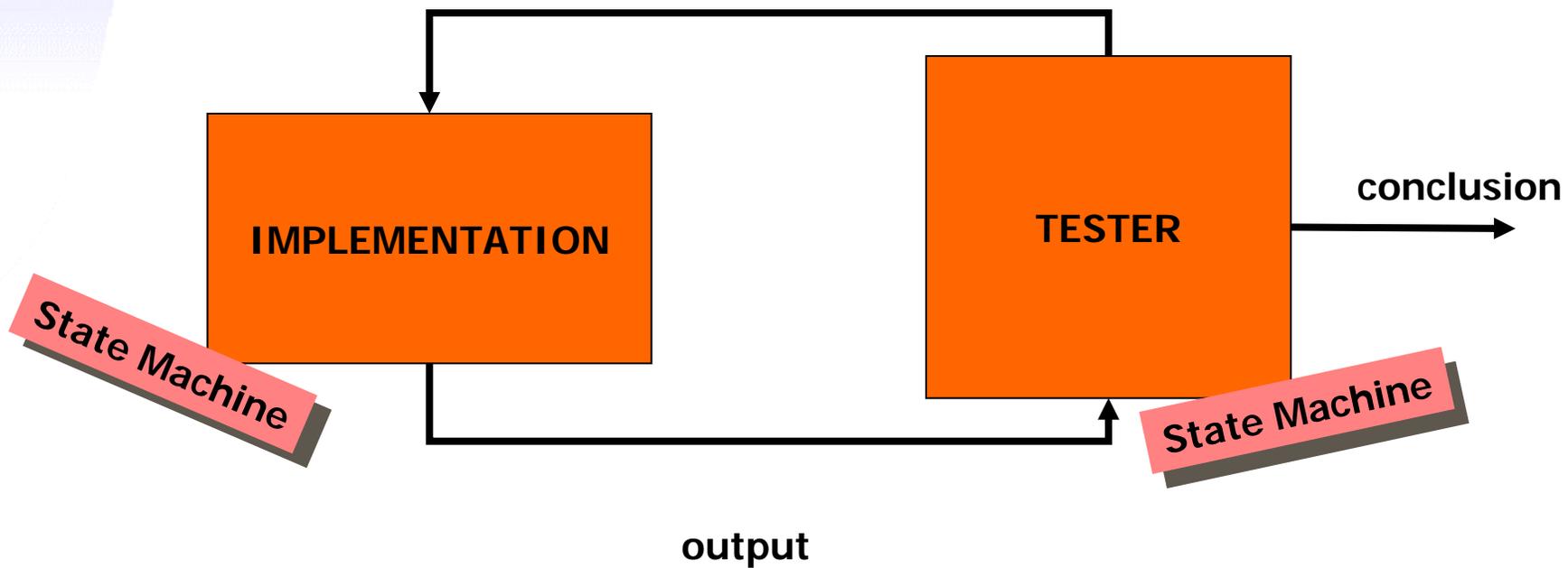
# Modelbased Testing

# Motivation

- Testing = sample executions of system compared with requirements
- Testing may identify errors but can not be used to exclude their presence.
- Testing is the de-facto used method of validation
- 30-40% of the entire development process is concerned with testing.

# Black Box Testing

input stimuli



output

conclusion

IMPLEMENTATION

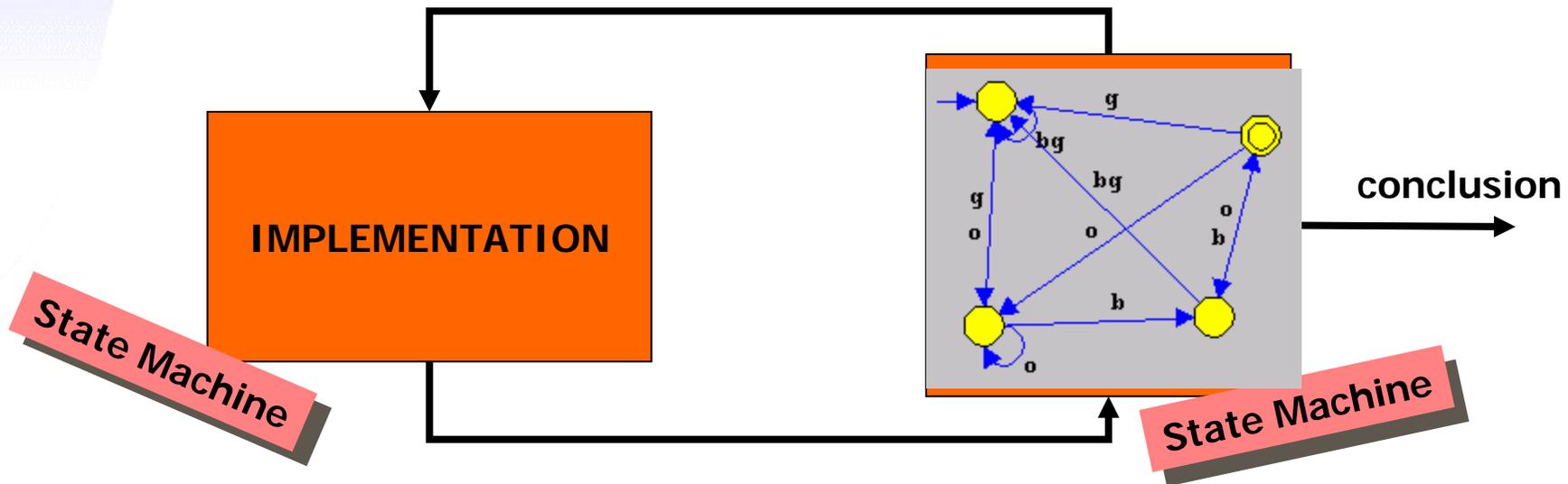
TESTER

State Machine

State Machine

# Black Box Testing

input stimuli



IMPLEMENTATION

State Machine

State Machine

conclusion

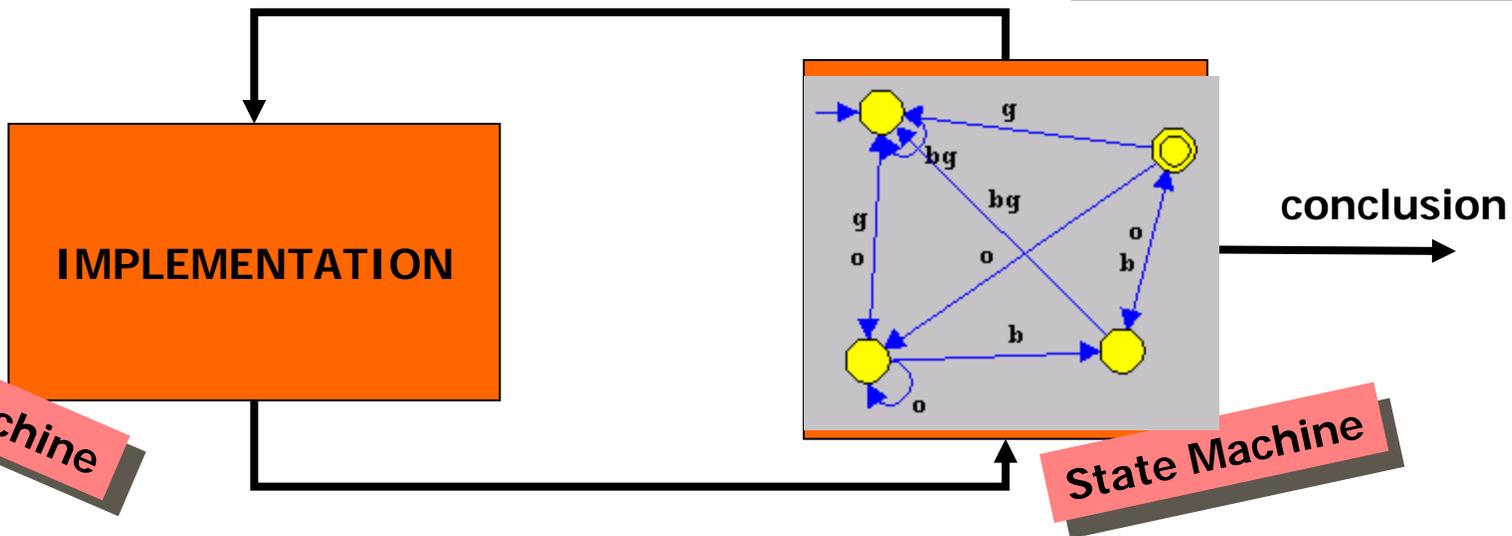
output  
closed/open

TEST	EXPECTED OUTPUT
gogoobb	closed
goobo	open
ggggggggg	closed
ooooggobo	open
.....	....

# Black Box Testing

**MOORE's Theorem:**  
Hvis IMP antages at have  $m$  tilstande og SPEC har  $n$  tilstande da er det nok at teste mht alle sekvenser af lgd  $n+m-1$

input stimuli



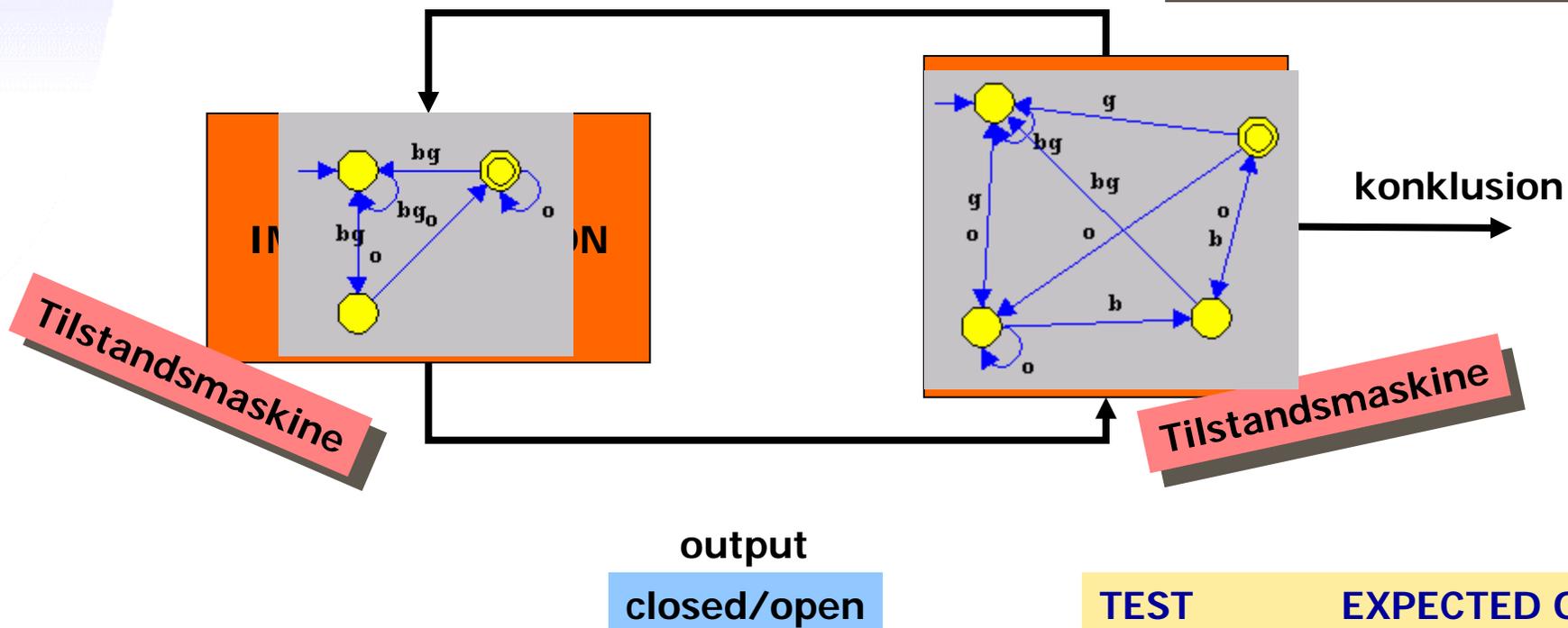
output  
closed/open

TEST	EXPECTED OUTPUT
gogoobb	closed
goobo	open
ggggggggg	closed
ooooggobo	open
.....	....

# Black Box Testing

input stimuli

**MOORE's Theorem:**  
Hvis IMP antages at have  $m$  tilstande og SPEC har  $n$  tilstande da er det nok at teste mht alle sekvenser af lgd  $n+m-1$

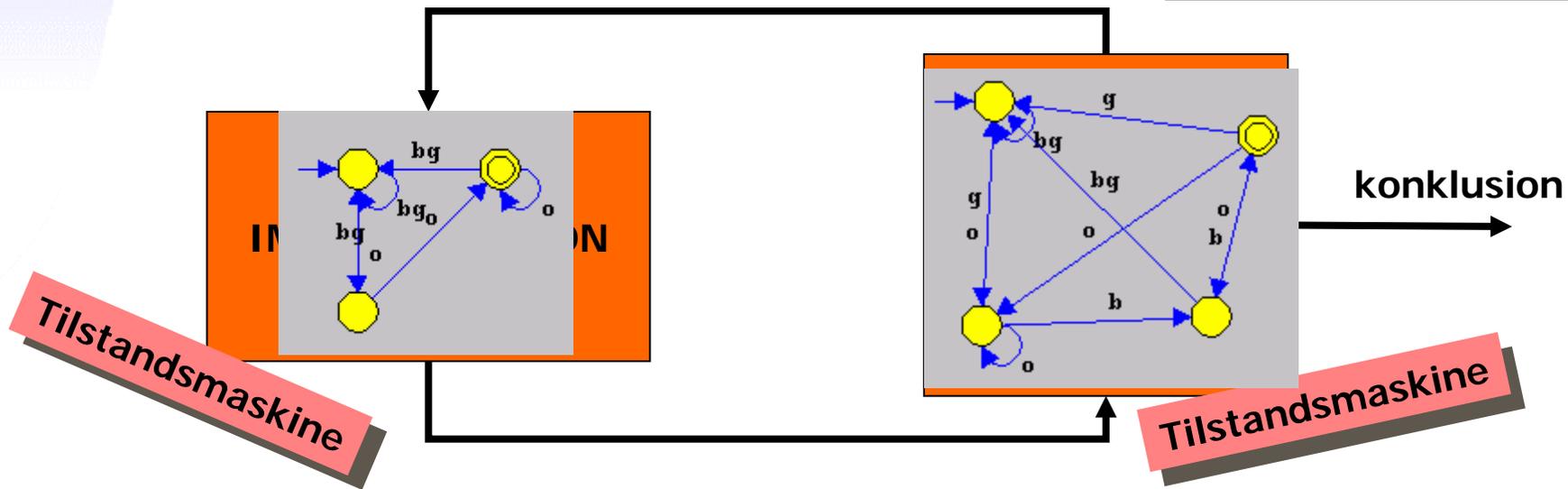


TEST	EXPECTED OUTPUT
ggggobo	open (closed)
gggggoo	closed (open)
.....	...
.....	...
.....	....

# Black Box Testing

input stimuli

**MOORE's Theorem:**  
Hvis IMP antages at have  $m$  tilstande og SPEC har  $n$  tilstande da er det nok at teste mht alle sekvenser af lgd  $n+m-1$



Tilstandsmaskine

Tilstandsmaskine

**Problem:**  
Antal test er  
**ASTRONOMISK:**  
 $k^{(n+m-1)}$   
hvor  $k$  er antal symboler

output  
closed/open

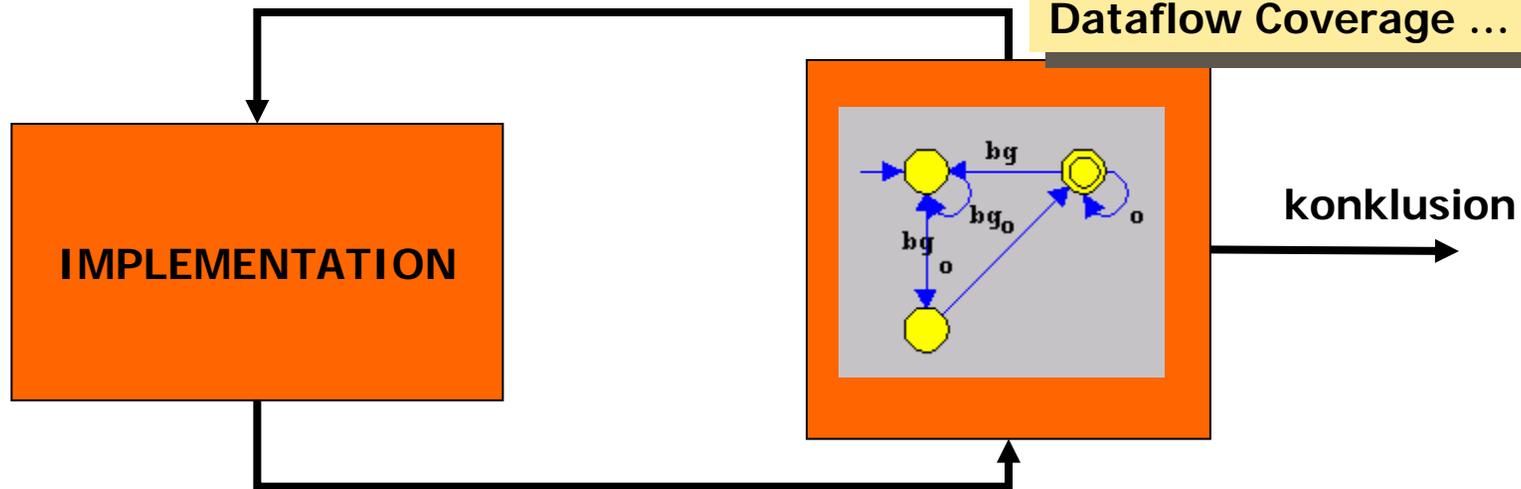
TEST	EXPECTED OUTPUT
ggggobo	open (closed)
gggggoo	closed (open)
.....	...
.....	...
.....	....

# Black Box Testing

input stimuli

## Control Flow Coverage

Enhver transition skal fyres  
Enhver (lokal) tilstand skal nås  
Enhver (ikke-triviell) guard skal kunne være både sand/falsk  
Dataflow Coverage ...



output

closed/open

## Problem:

Coverage kun af specifikation – implementation behøver kun at være dækket ganske lidt!

## Løsning:

Brug specifikation automata til at (randomiseret) stimulering og løbende check konsistens af implementations reaktion

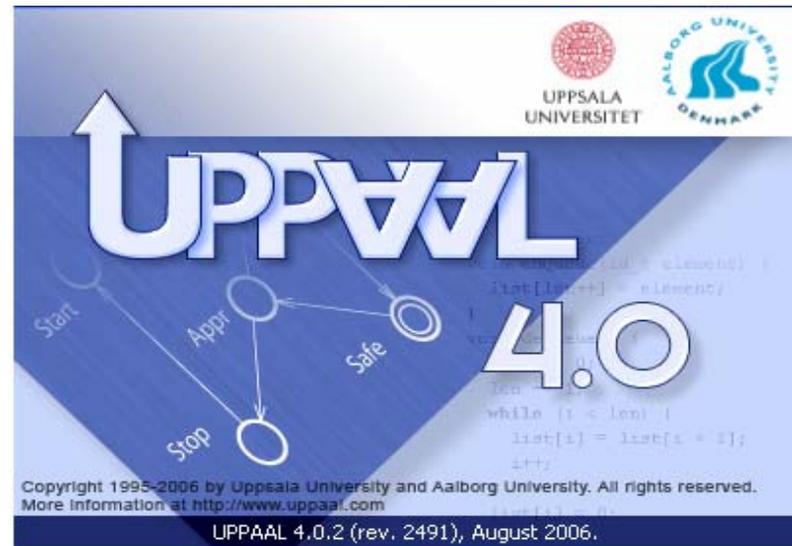
UPPAAL Tron

# Adding Time

**FSM**



**Timed Automata**



# Collaborators

## @UPPsala

- Wang Yi
- Paul Pettersson
- John Håkansson
- Anders Hessel
- Pavel Krcal
- Leonid Mokrushin
- Shi Xiaochun

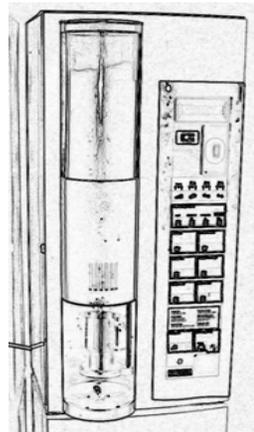
## @AALborg

- Kim G Larsen
- Gerd Behrman
- Arne Skou
- Brian Nielsen
- Alexandre David
- Jacob Illum Rasmussen
- Marius Mikucionis

## @Elsewhere

- Emmanuel Fleury, Didier Lime, Johan Bengtsson, Fredrik Larsson, Kåre J Kristoffersen, Tobias Amnell, Thomas Hune, Oliver Möller, Elena Fersman, Carsten Weise, David Griffioen, Ansgar Fehnker, Frits Vandraager, Theo Ruys, Pedro D'Argenio, J-P Katoen, Jan Tretmans, Judi Romijn, Ed Brinksma, Martijn Hendriks, Klaus Havelund, Franck Cassez, Magnus Lindahl, Francois Laroussinie, Patricia Bouyer, Augusto Burgueno, H. Bowmann, D. Latella, M. Massink, G. Faconti, Kristina Lundqvist, Lars Asplund, Justin Pearson...

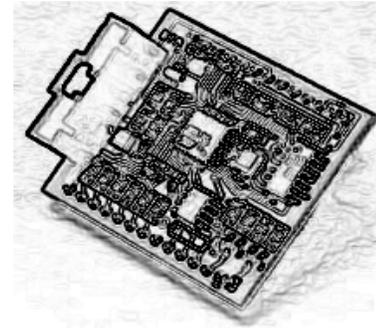
# Real Time Systems



**Plant**  
*Continuous*

sensors →

← actuators



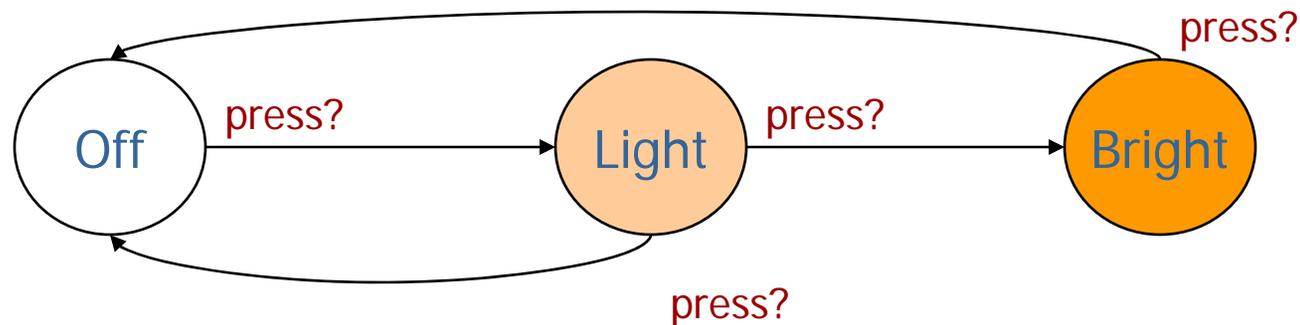
**Controller Program**  
*Discrete*

- Eg.:** Realtime Protocols  
 Pump Control  
 Air Bags  
 Robots  
 Cruise Control  
 ABS  
 CD Players  
 Production Lines

## Real Time System

A system where correctness not only depends on the logical order of events but also on their **timing!!**

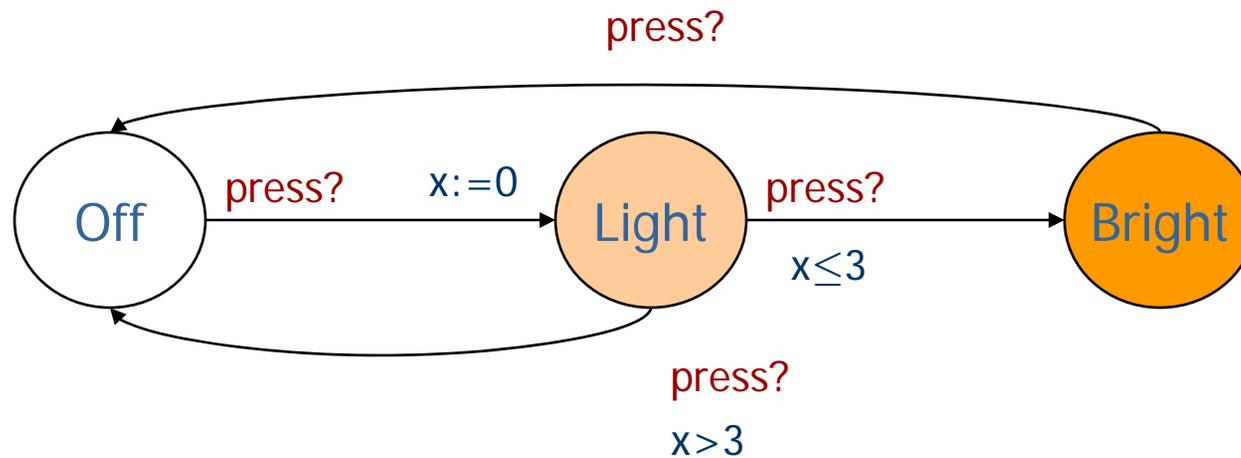
# Dumb Light Control



**WANT:** if **press** is issued twice **quickly** then the **light** will get **brighter**; otherwise the light is turned **off**.

# Dumb Light Control

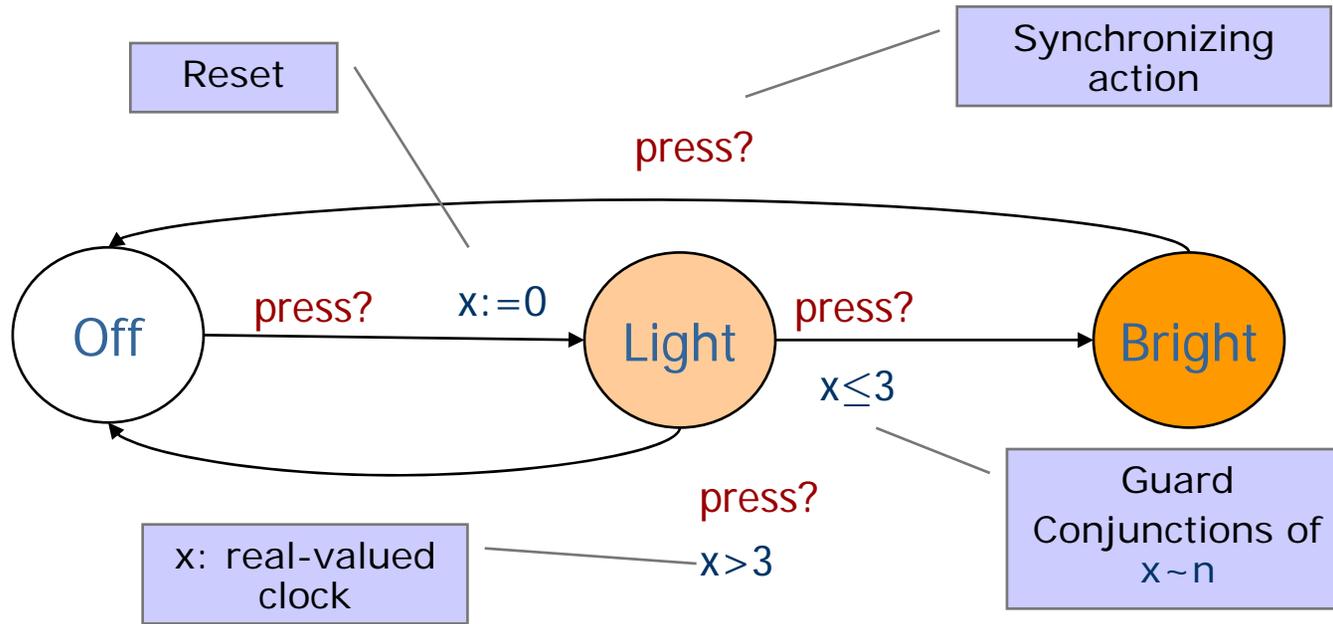
*Alur & Dill 1990*



**Solution:** Add real-valued clock **x**

# Timed Automata

*Alur & Dill 1990*



**States:**

( location ,  $x=v$  ) where  $v \in \mathbf{R}$

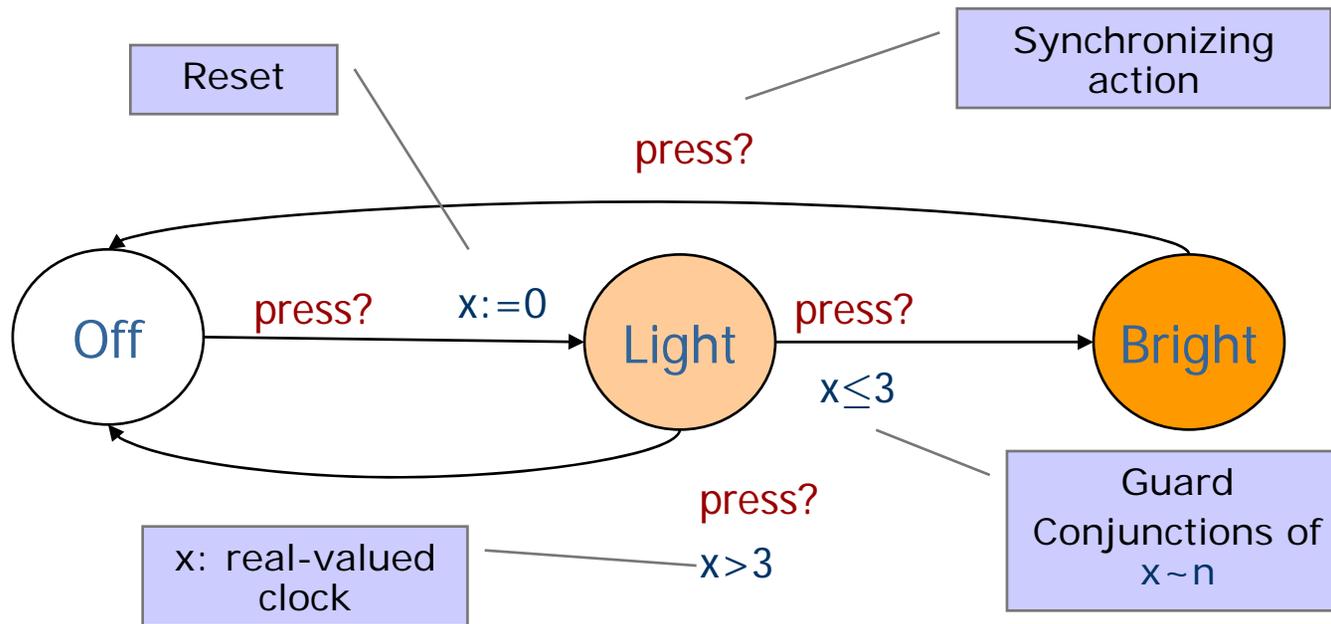
**Transitions:**

( Off ,  $x=0$  )



# Timed Automata

*Alur & Dill 1990*



**States:**

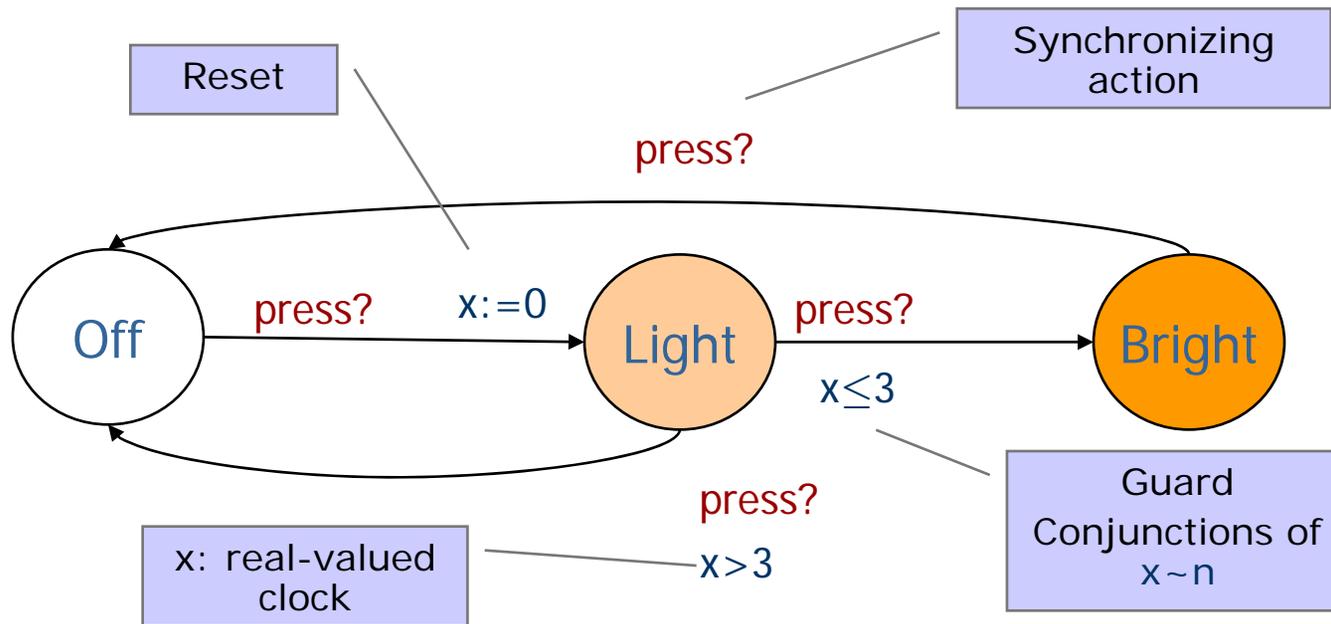
( location ,  $x=v$  ) where  $v \in \mathbf{R}$

**Transitions:**

( Off ,  $x=0$  )  
 delay 4.32                       $\rightarrow$  ( Off ,  $x=4.32$  )  
 press?                               $\rightarrow$  ( Light ,  $x=0$  )

# Timed Automata

*Alur & Dill 1990*



**States:**

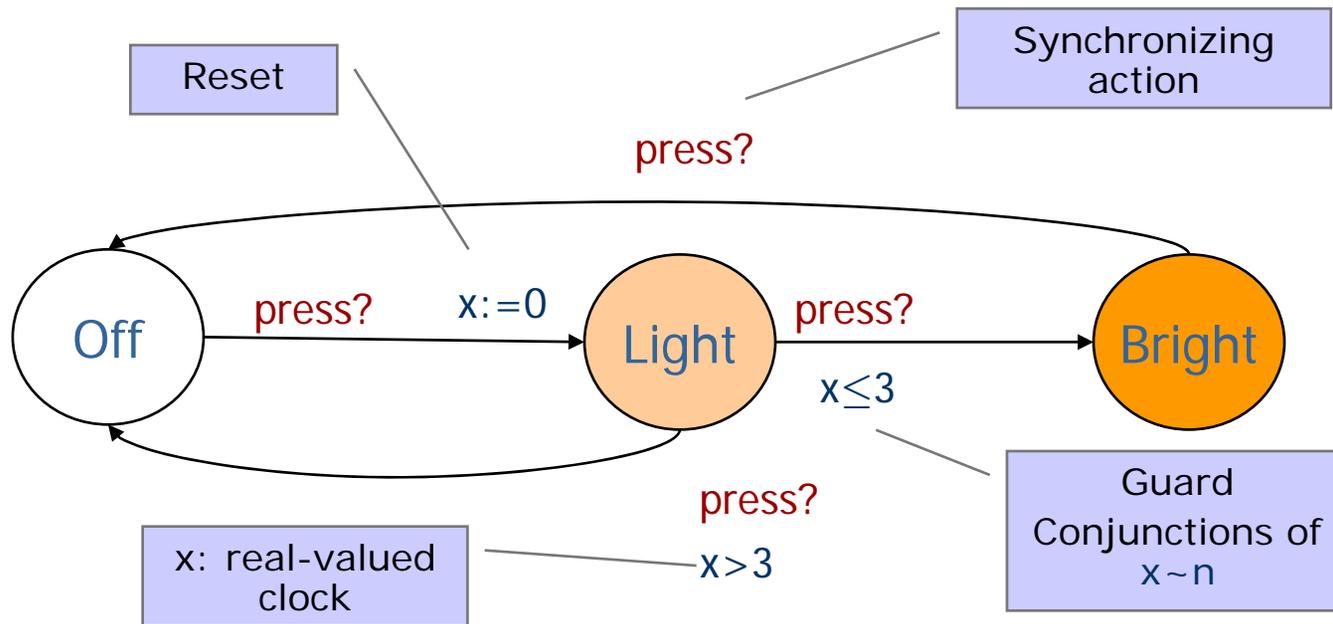
( location ,  $x=v$  ) where  $v \in \mathbf{R}$

**Transitions:**

( Off ,  $x=0$  )  
 delay 4.32  $\rightarrow$  ( Off ,  $x=4.32$  )  
 press?  $\rightarrow$  ( Light ,  $x=0$  )  
 delay 2.51  $\rightarrow$  ( Light ,  $x=2.51$  )

# Timed Automata

*Alur & Dill 1990*



## States:

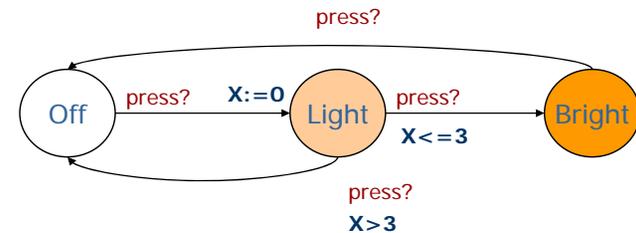
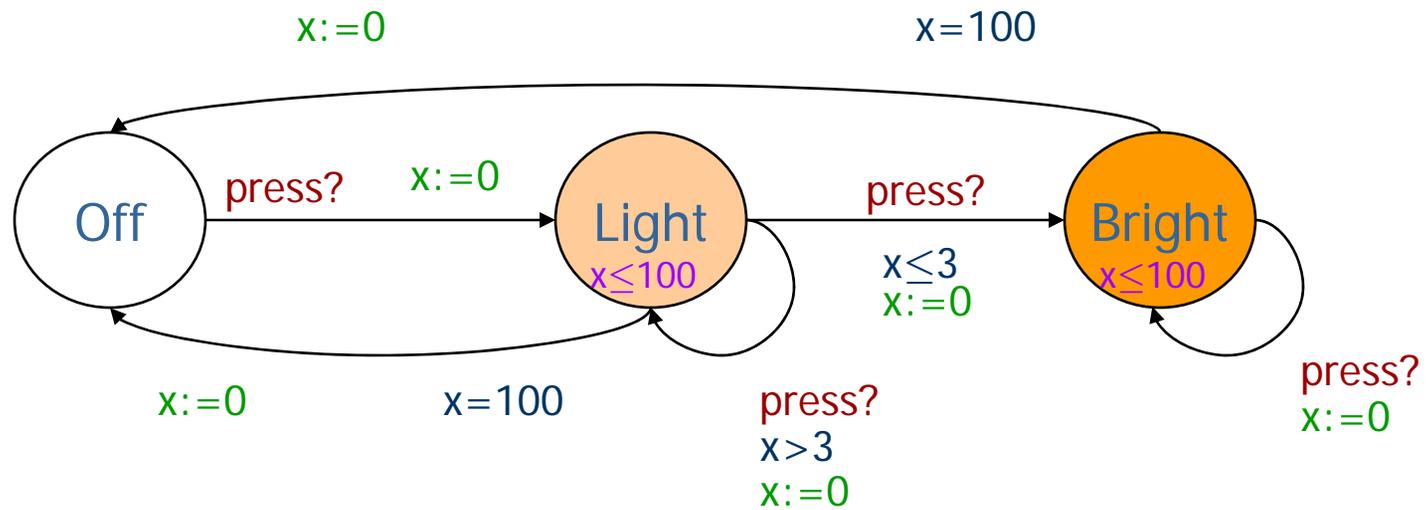
( location ,  $x=v$  ) where  $v \in \mathbf{R}$

## Transitions:

	( Off , $x=0$ )
delay 4.32	$\rightarrow$ ( Off , $x=4.32$ )
$\text{press?}$	$\rightarrow$ ( Light , $x=0$ )
delay 2.51	$\rightarrow$ ( Light , $x=2.51$ )
$\text{press?}$	$\rightarrow$ ( Bright , $x=2.51$ )

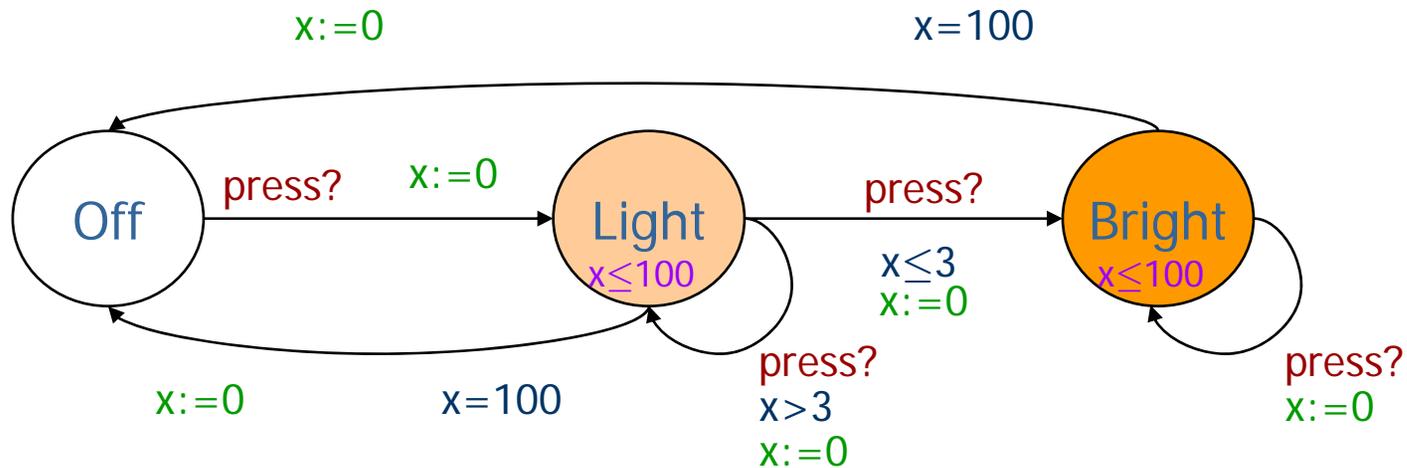
# Intelligent Light Control

Using Invariants



# Intelligent Light Control

Using Invariants



**Transitions:**

- delay 4.32       $( \text{Off} , x=0 ) \rightarrow ( \text{Off} , x=4.32 )$
- press?         $\rightarrow ( \text{Light} , x=0 )$
- delay 4.51       $\rightarrow ( \text{Light} , x=4.51 )$
- press?         $\rightarrow ( \text{Light} , x=0 )$
- delay 100        $\rightarrow ( \text{Light} , x=100 )$
- $\tau$               $\rightarrow ( \text{Off} , x=0 )$

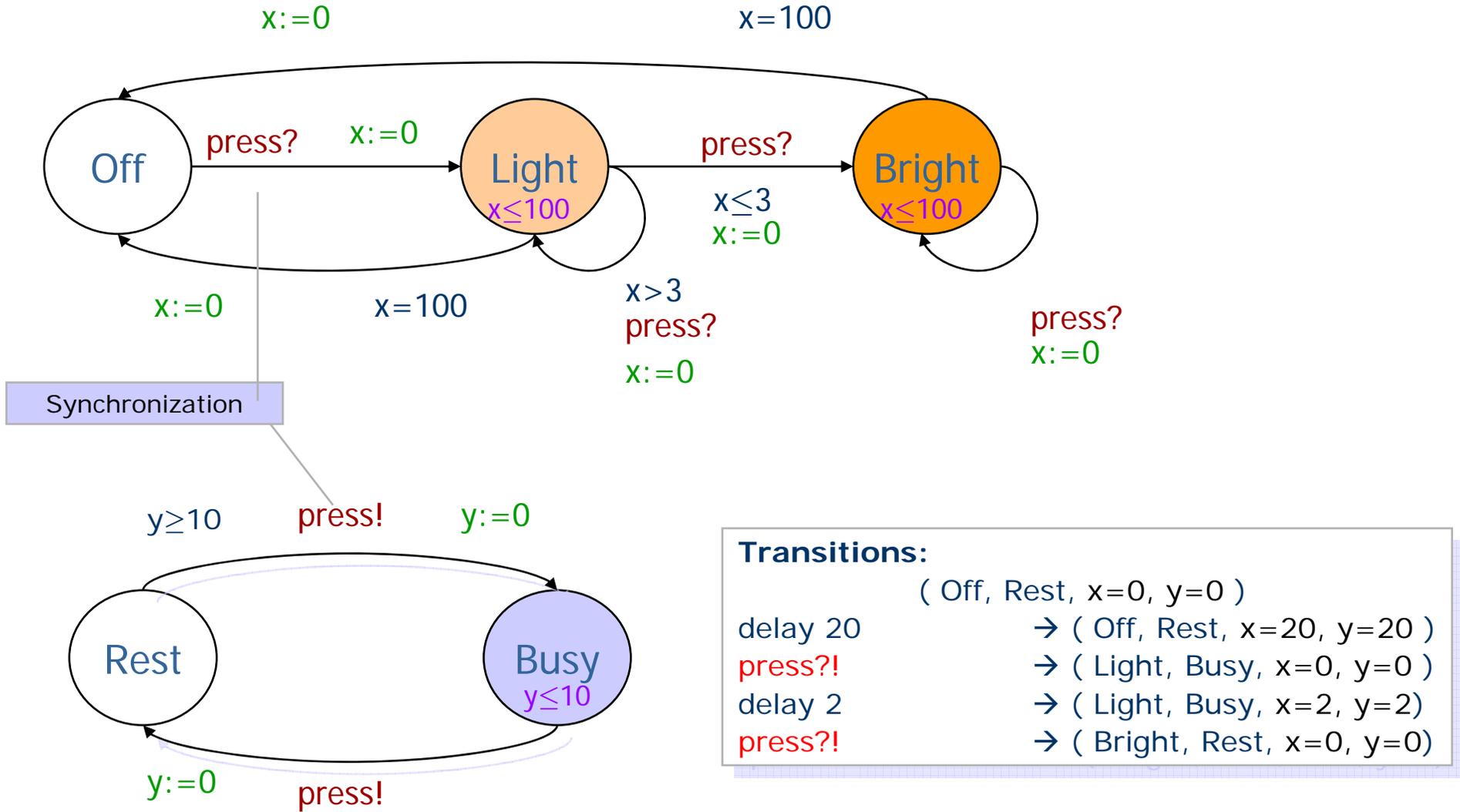
**Note:**

$( \text{Light} , x=0 ) \text{ delay } 103 \rightarrow$

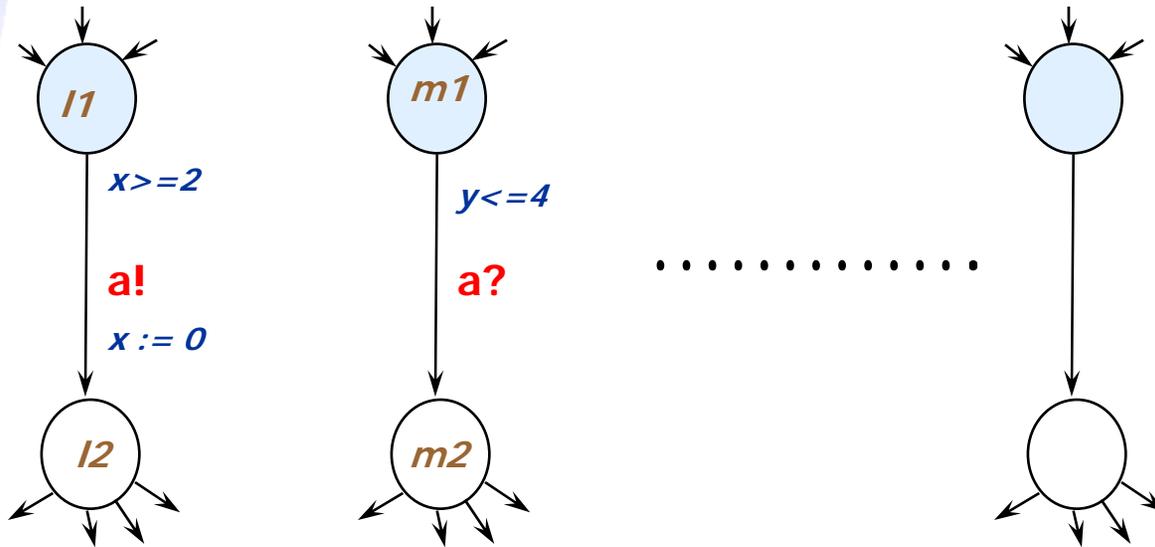


Invariants ensures progress

# Networks Light Controller & User

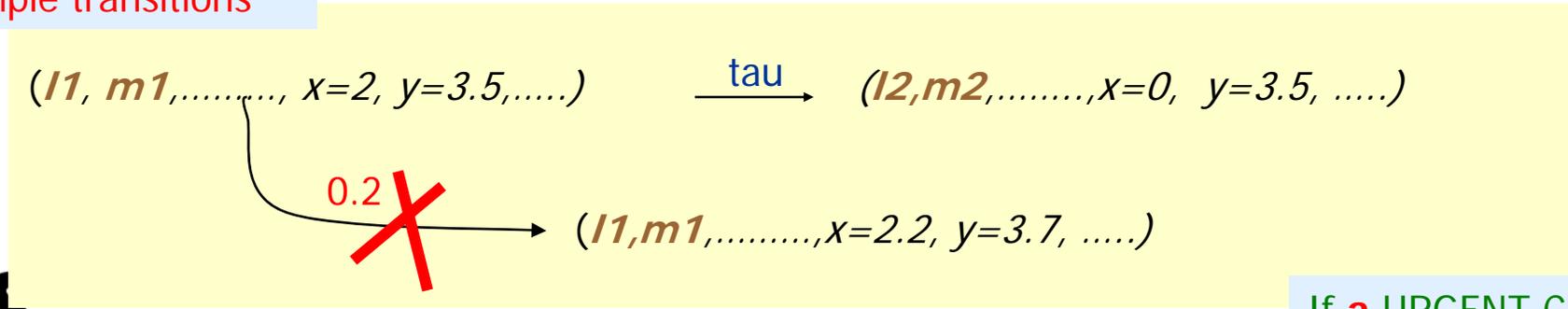


# Networks of Timed Automata (a'la CCS)



Two-way synchronization on *complementary* actions.  
**Closed Systems!**

**Example transitions**

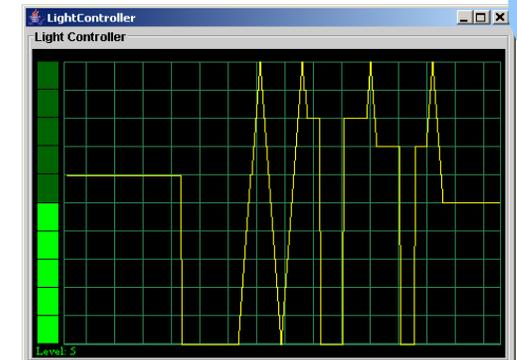
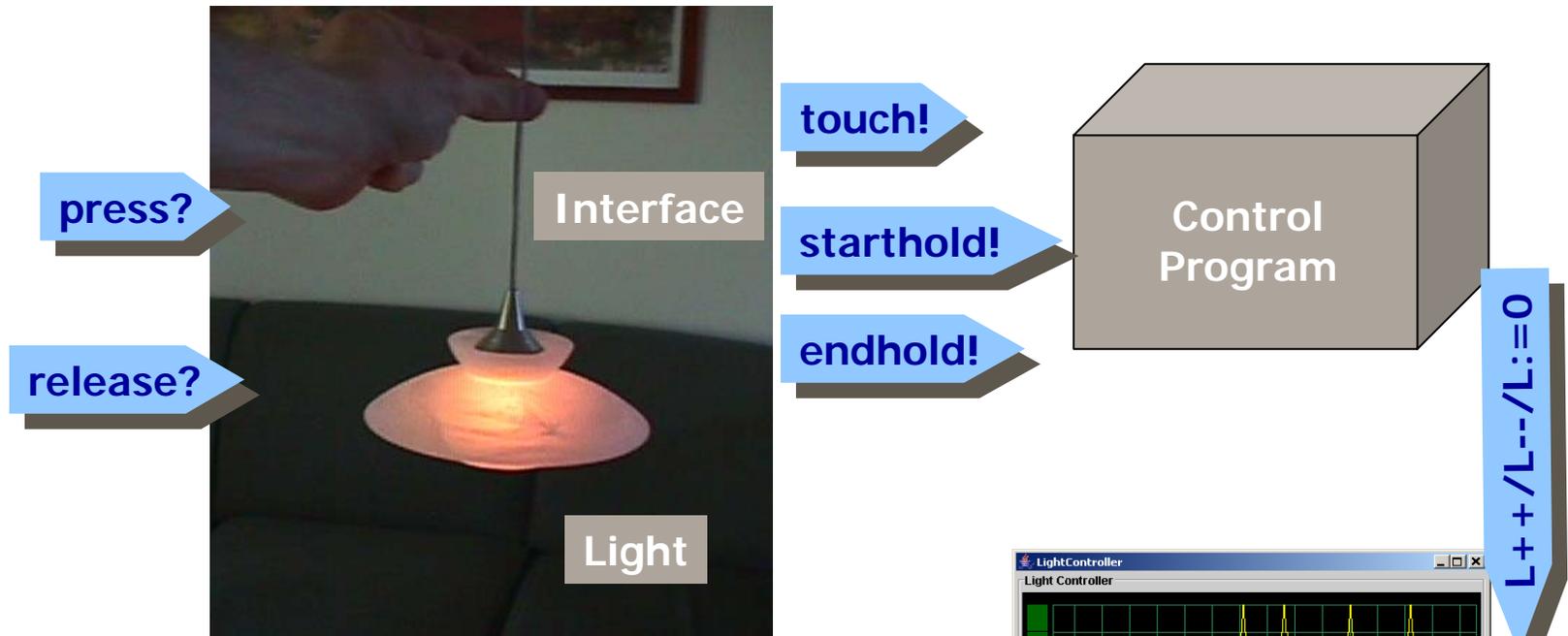


If **a** URGENT CHANNEL

# Light Control Interface



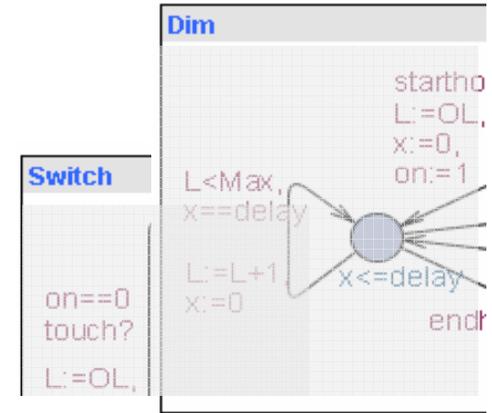
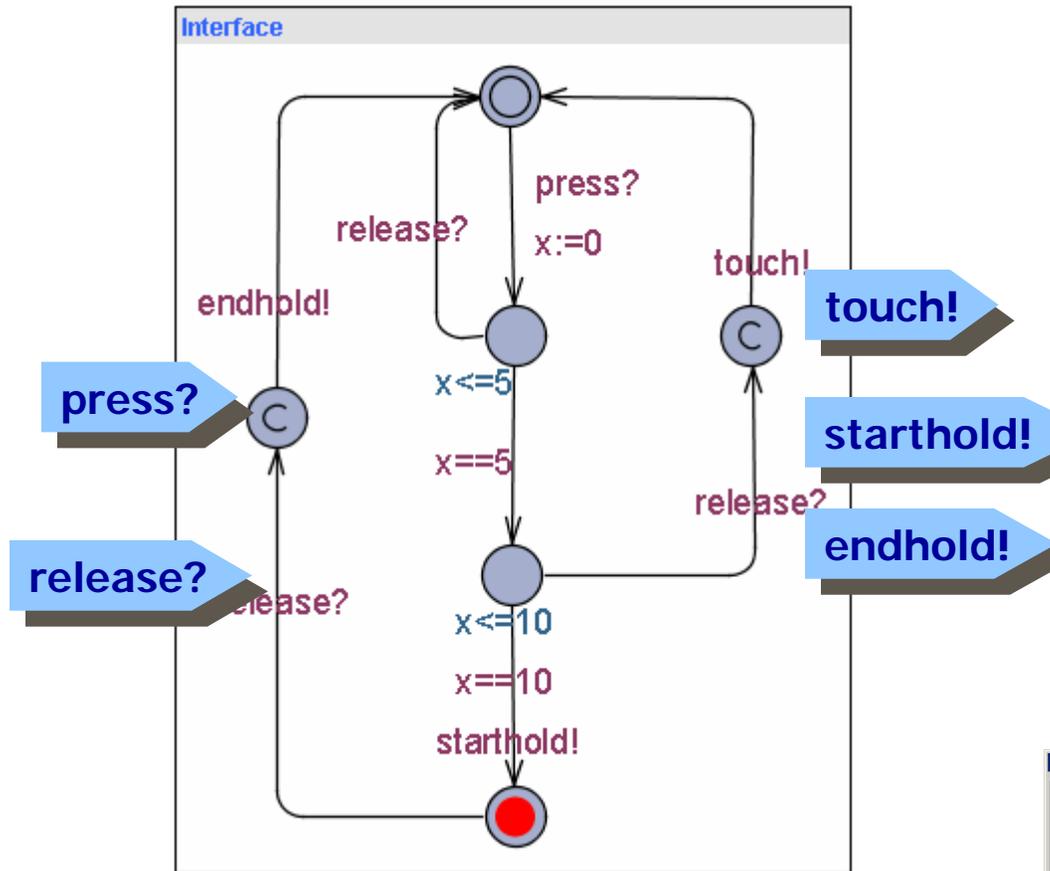
User



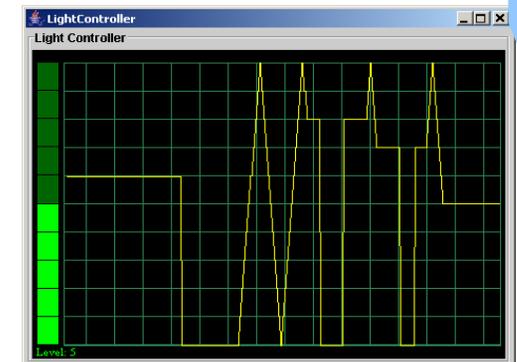
# Light Control Interface



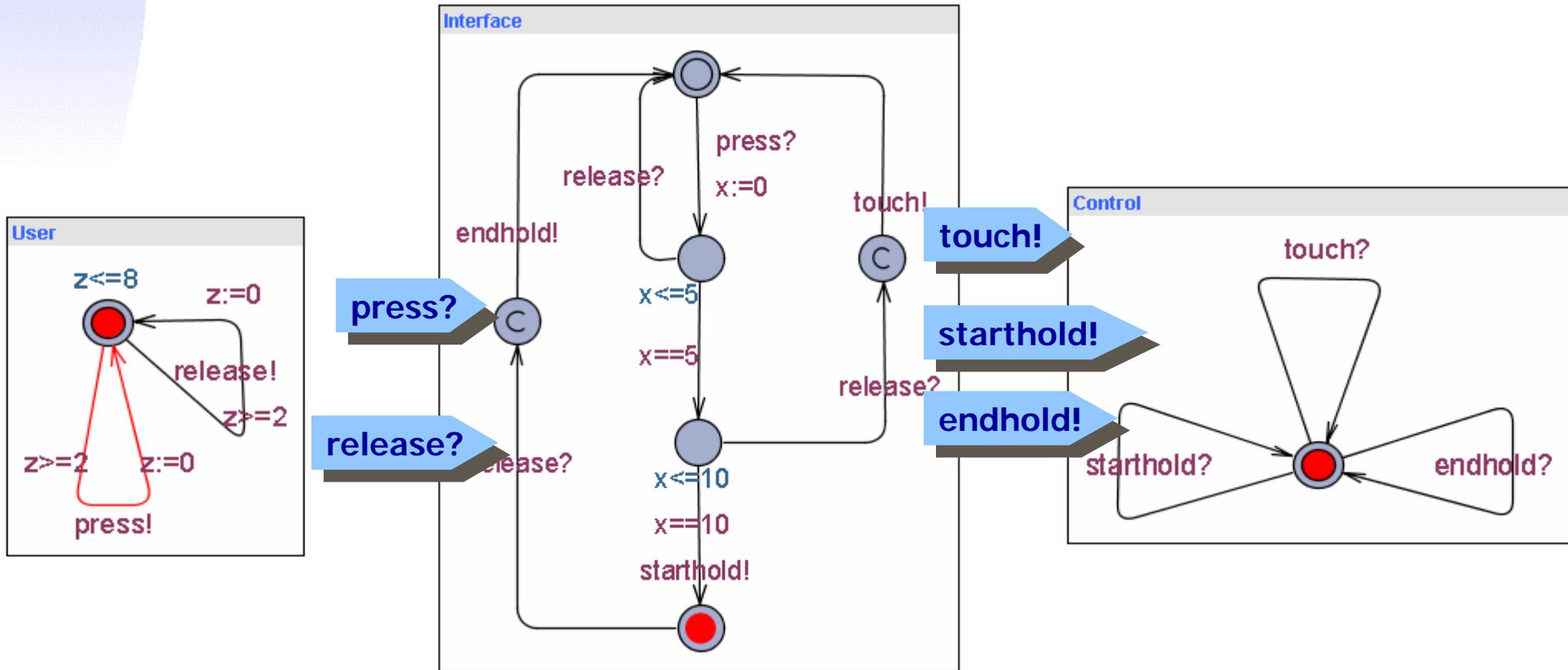
User



L++/L--/L:=0



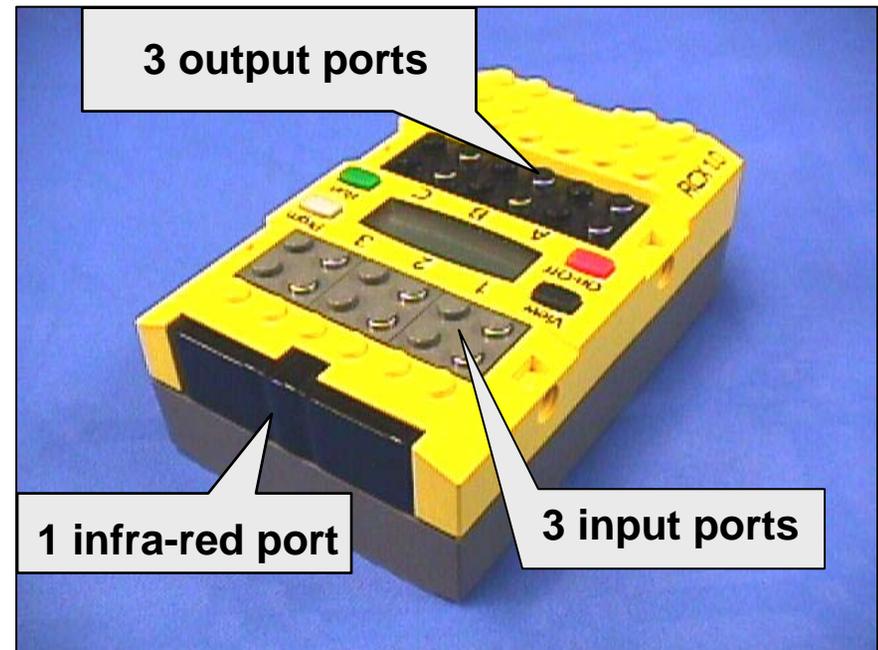
# Light Control Network



# **BRICK SORTING**

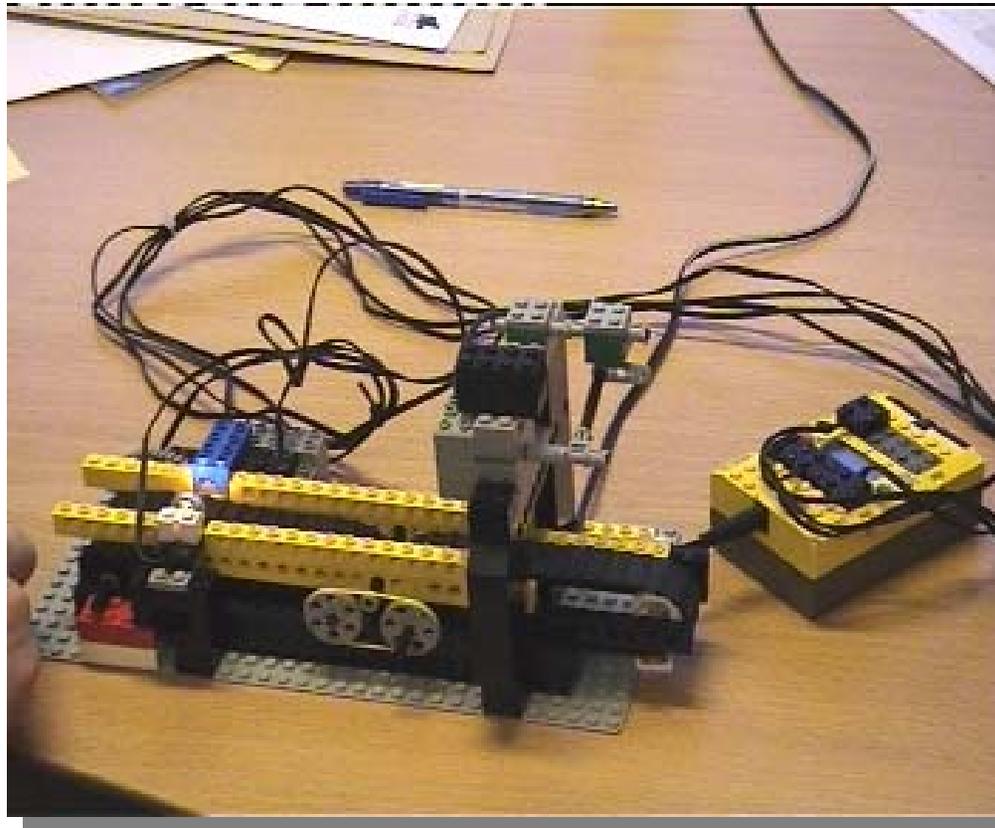
# LEGO Mindstorms/RCX

- Sensors: temperature, light, rotation, pressure.
- Actuators: motors, lamps,
- Virtual machine:
  - 10 tasks, 4 timers, 16 integers.
- Several Programming Languages:
  - NotQuiteC, Mindstorm, Robotics, legOS, etc.



# A Real Timed System

**The Plant**  
Conveyor Belt  
&  
Bricks



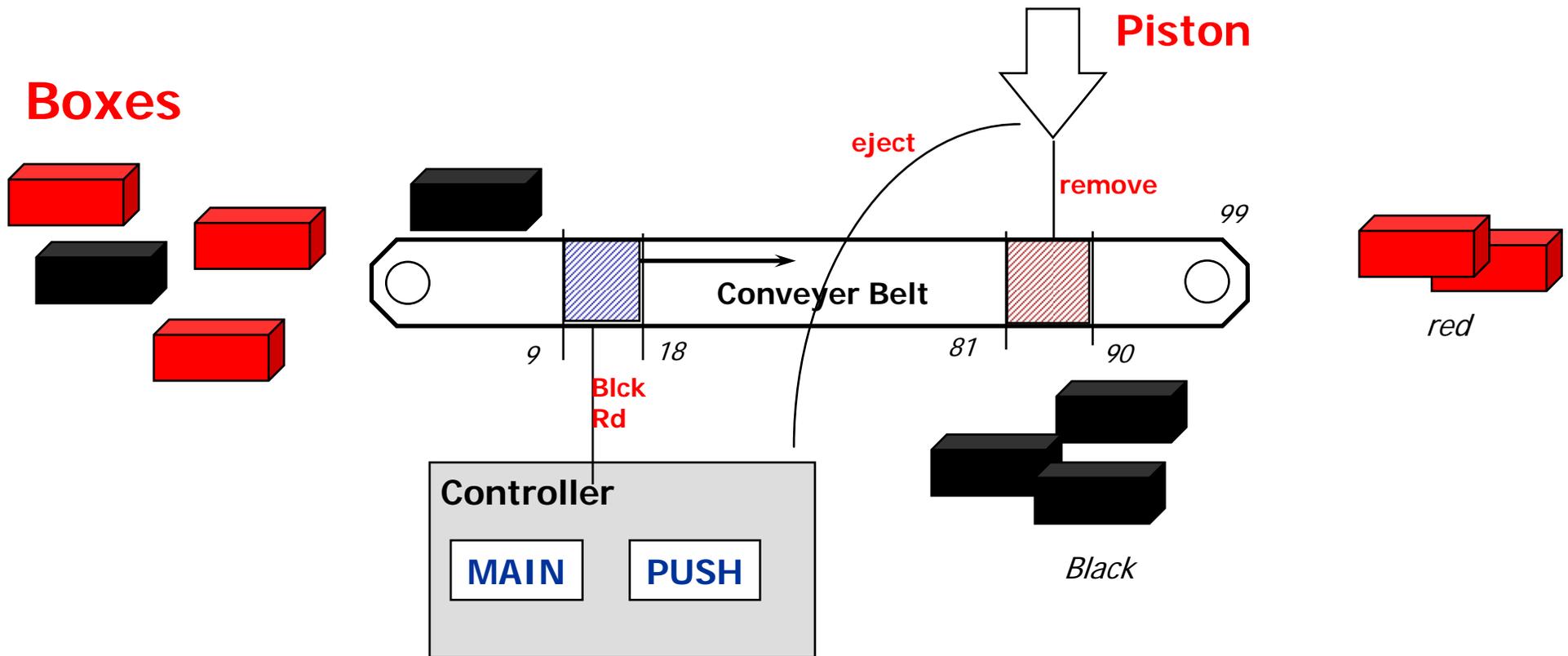
**Controller  
Program**  
LEGO MINDSTORM

**What is suppose to happen?**

# First UPPAAL model

*Sorting of Lego Boxes*

Ken Tindell



**Exercise:** Design **Controller** so that only black boxes are being pushed out

# NQC programs

```
int active;
int DELAY;
int LIGHT_LEVEL;
```

```
task MAIN{
  DELAY=75;
  LIGHT_LEVEL=35;
  active=0;
  Sensor(IN_1, IN_LIGHT);
  Fwd(OUT_A,1);
  Display(1);

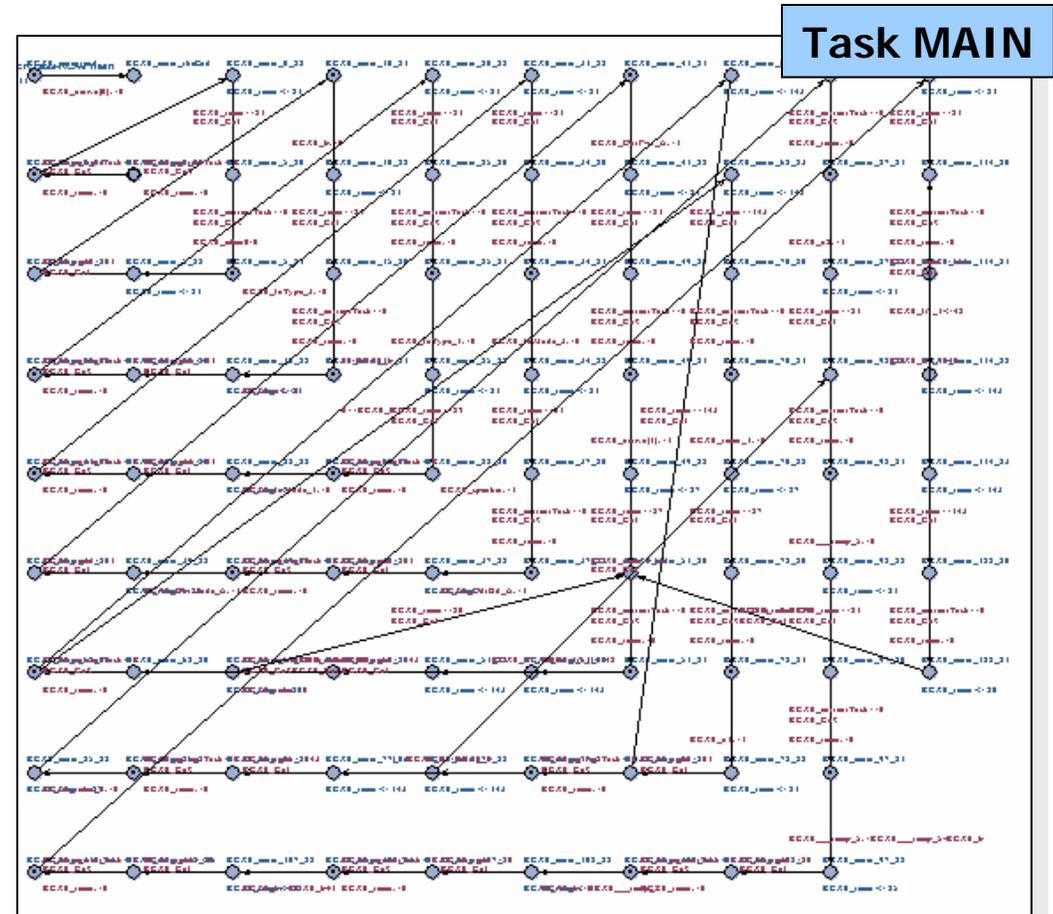
  start PUSH;

  while(true){
    wait(IN_1<=LIGHT_LEVEL);
    ClearTimer(1);
    active=1;
    PlaySound(1);
    wait(IN_1>LIGHT_LEVEL);
  }
}
```

```
task PUSH{
  while(true){
    wait(Timer(1)>DELAY && active==1);
    active=0;
    Rev(OUT_C,1);
    Sleep(8);
    Fwd(OUT_C,1);
    Sleep(12);
    Off(OUT_C);
  }
}
```

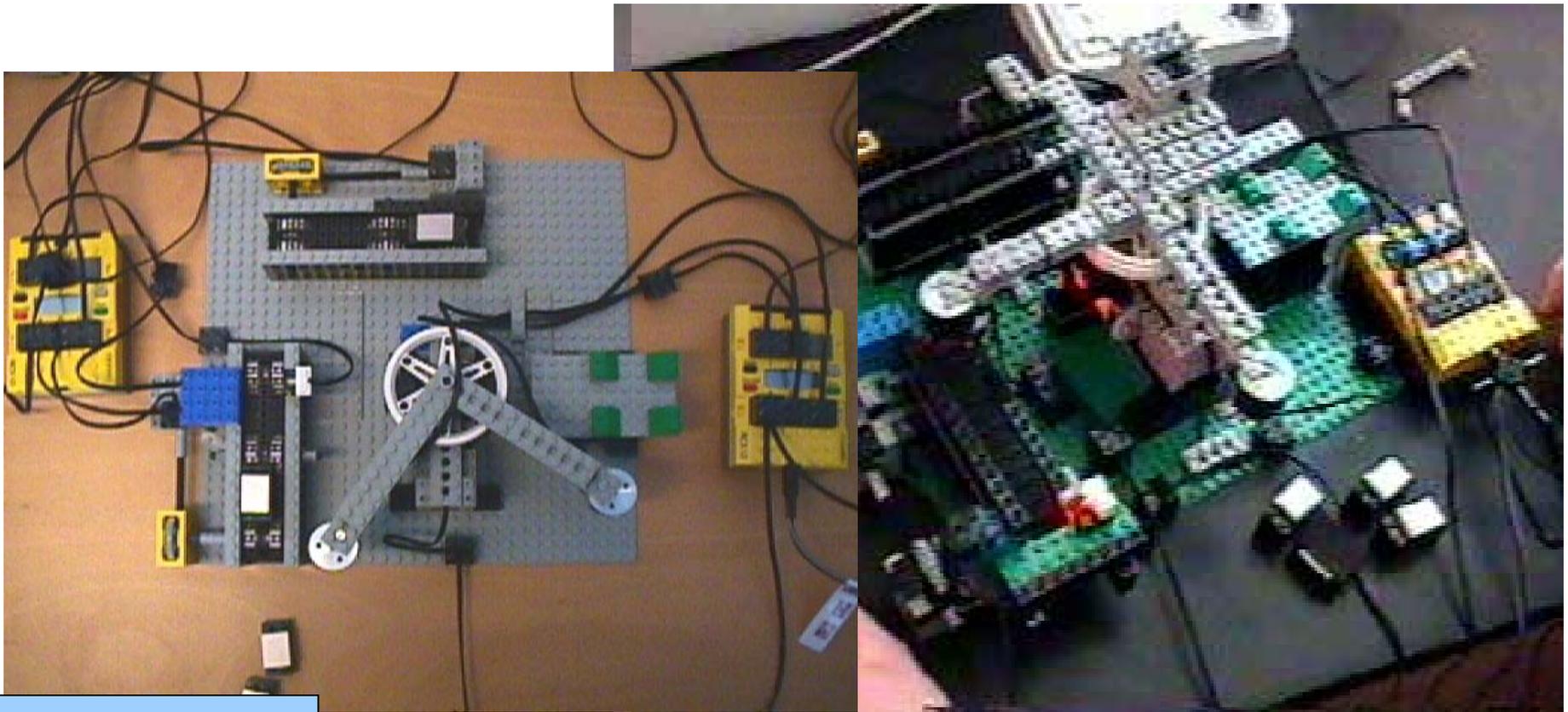
# From RCX to UPPAAL

- Model includes Round-Robin Scheduler.
- Compilation of RCX tasks into TA models.
- Presented at ECRTS 2000



# The Production Cell

*Course at DTU, Copenhagen*



**Production Cell**